



Determination of the Strong Coupling Constant from Inclusive Jet Production Cross Section and Double Parton Interactions in $\gamma+3$ -jets events

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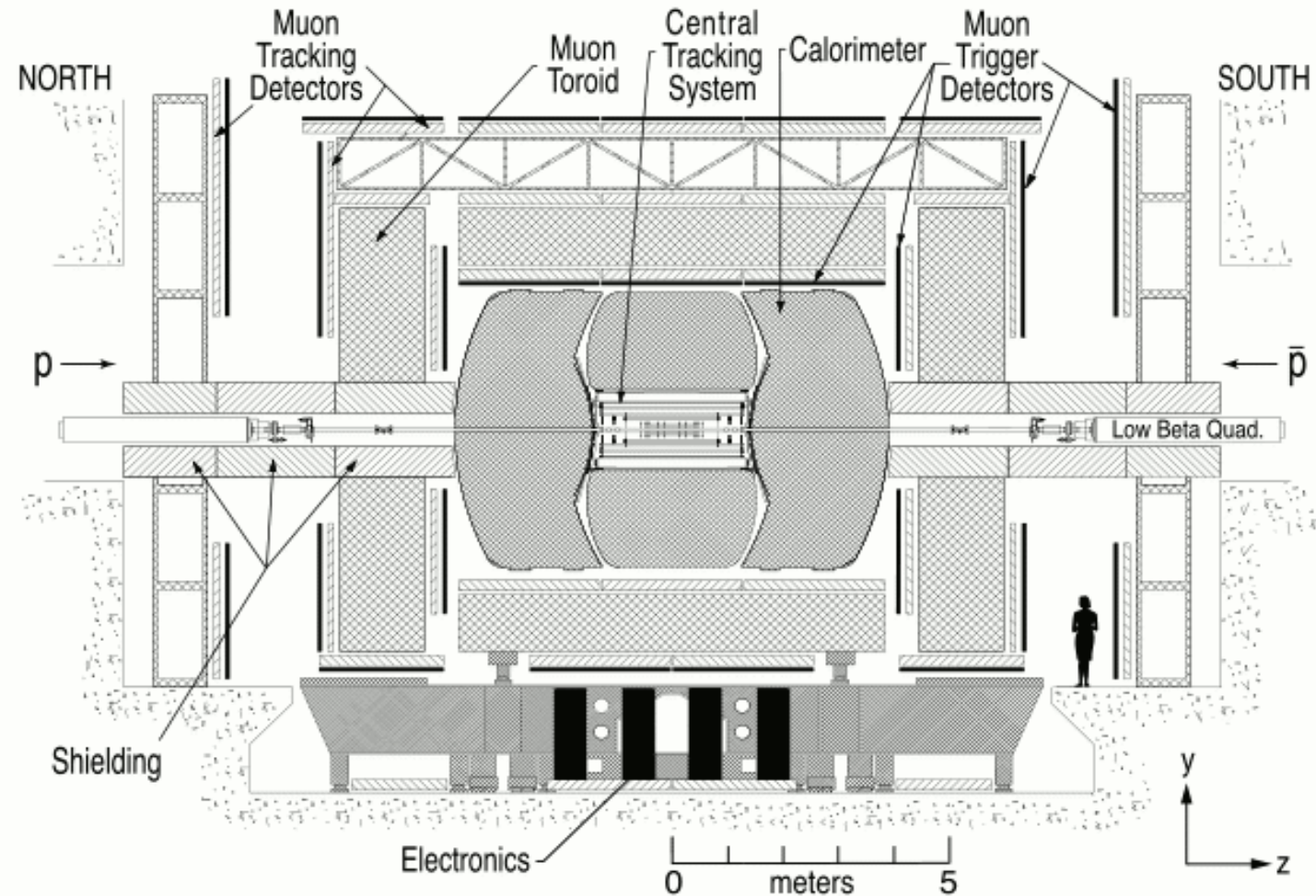
on behalf of the DØ Collaboration

Fermilab Joint Experimental-Theoretical Physics Seminar
December 11, 2009

Outline

- ◆ Dzero detector
- ◆ Determination of the Strong Coupling Constant from Inclusive Jet Production Cross Section.
- ◆ Double Parton Interactions in $\gamma+3$ -jets events; measurements of fraction of Double Parton events and effective cross section σ_{eff} .
- ◆ Summary

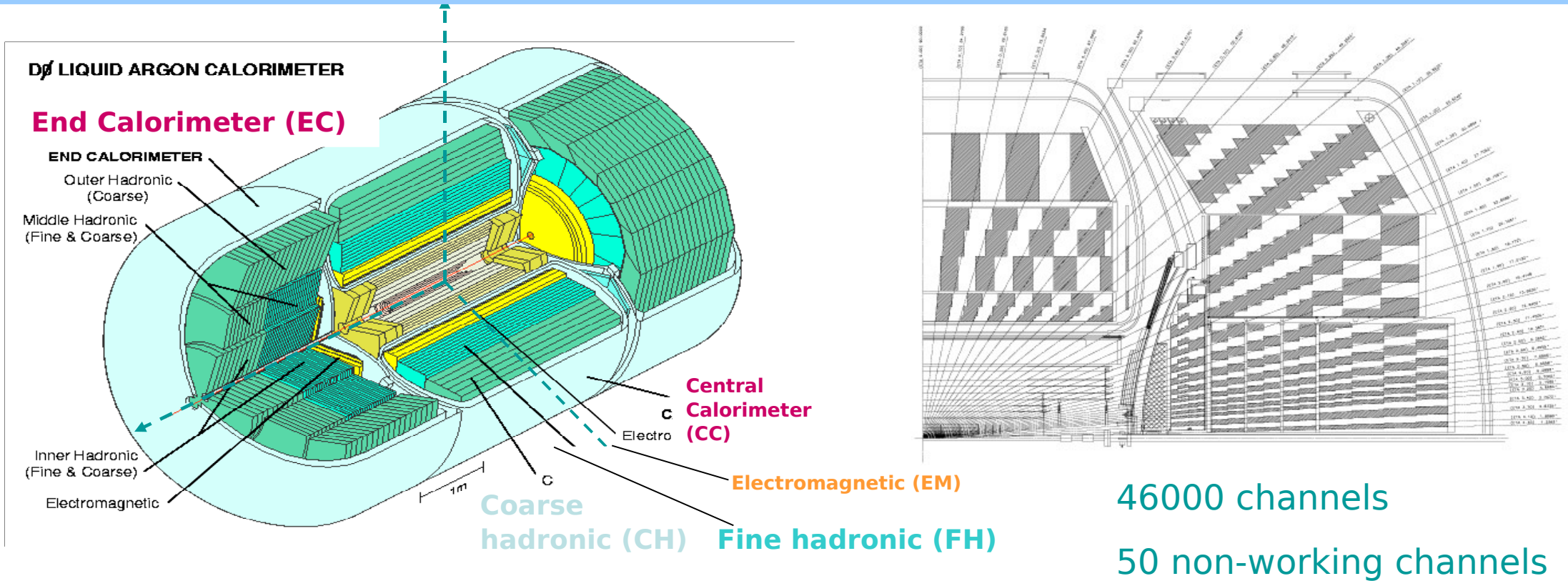
The Dzero detector



Three main systems

- Tracker (silicon and scintillating fibers)
- Calorimeter (LAr/U, some scintillators)
- Muon chambers and scintillators

Overview of the calorimeter

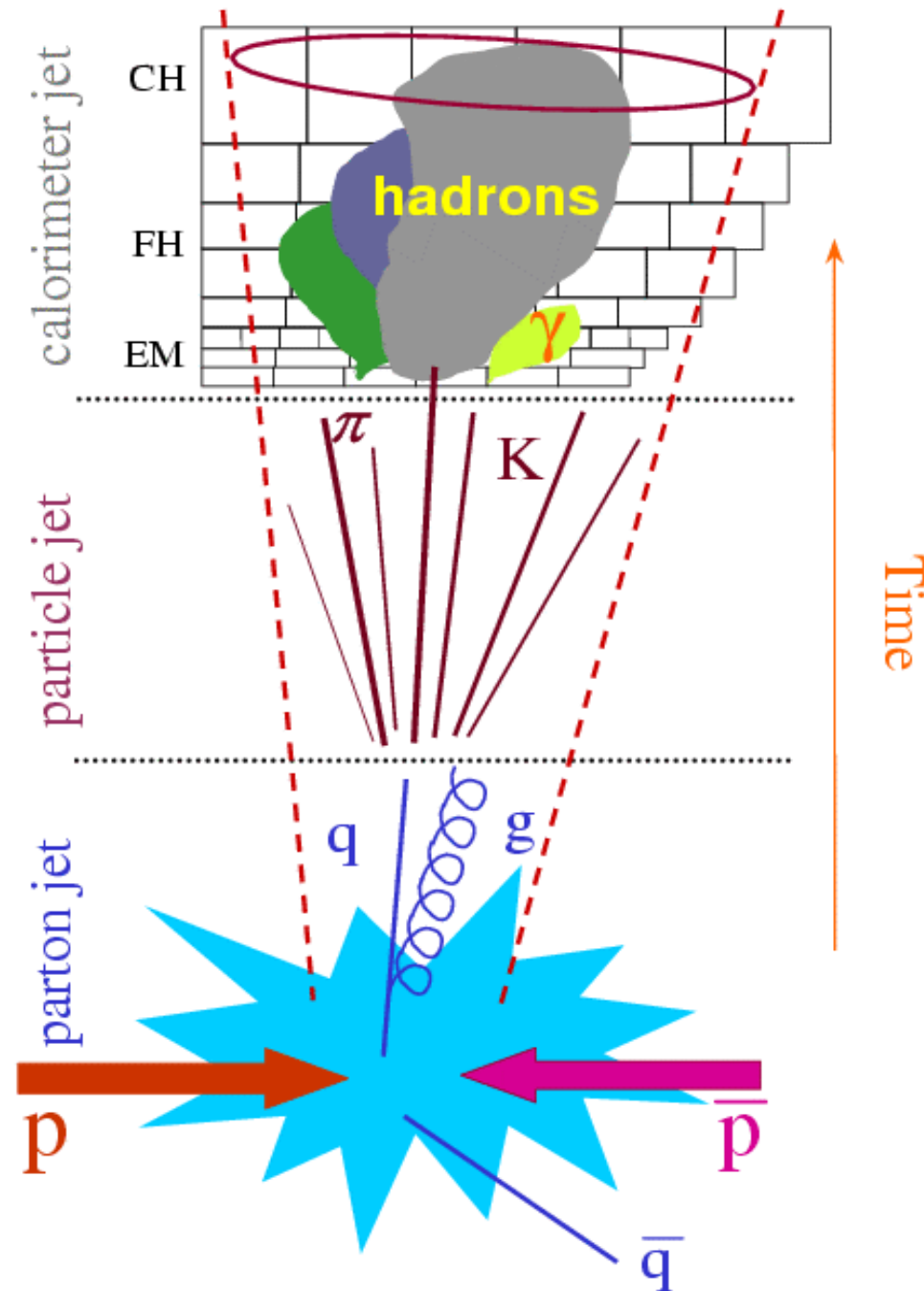


- ✓ Liquid argon active medium and (mostly) uranium absorber
- ✓ Hermetic with full coverage : $|\eta| < 4.2$
- ✓ Segmentation (towers): $\Delta\eta \times \Delta\Phi = 0.1 \times 0.1$ (0.05×0.05 in 3rd EM layer)
- ✓ Three main subregions: Central ($|\eta| < 1.1$), Intercryostat ($1.1 < |\eta| < 1.5$) and End calorimeters ($1.5 < |\eta| < 4.2$)
- ✓ Stable response, good resolution

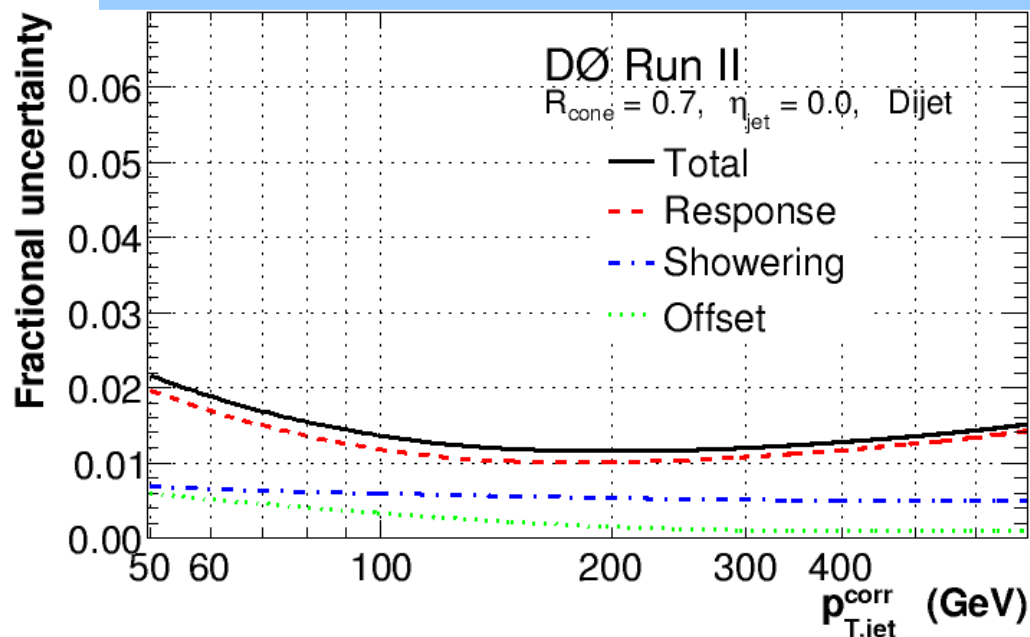
Jets, particles and partons

- We do not “see” partons or particles in calorimeter, only ADC counts
- ADC counts --> cell energies
- Run jet cone algorithm with

$$\Delta R = \sqrt{(\Delta y)^2 + (\Delta \Phi)^2} < R_{\text{cone}}$$
- Jet energy is corrected to the particle level using the Jet Energy Scale (JES) procedure :
- Calibrate using γ +jets, dijets and Z+jets
- JES includes: Energy Offset (energy not from the hard scattering process); Detector Response Out-of-Cone showering; Resolution



Energy scale uncertainty: 1-2% !



α_s Determination

- Motivations
- Data set
- Basic fit principle
- PDFs and α_s
- PDFs and input data
- Results

α_s and the RGE

- $\alpha_s(\mu_r)$ depends on renormalization scale μ_r
 - ✓ It is not predicted in QCD
 - ✓ It should be determined in experiment
- Renormalization Group Equation (RGE) predicts μ_r dependence
- The measured values of $\alpha_s(\mu_r)$ can be evolved to the mass of Z boson (common agreement) by using the solution to the 2-loop RGE

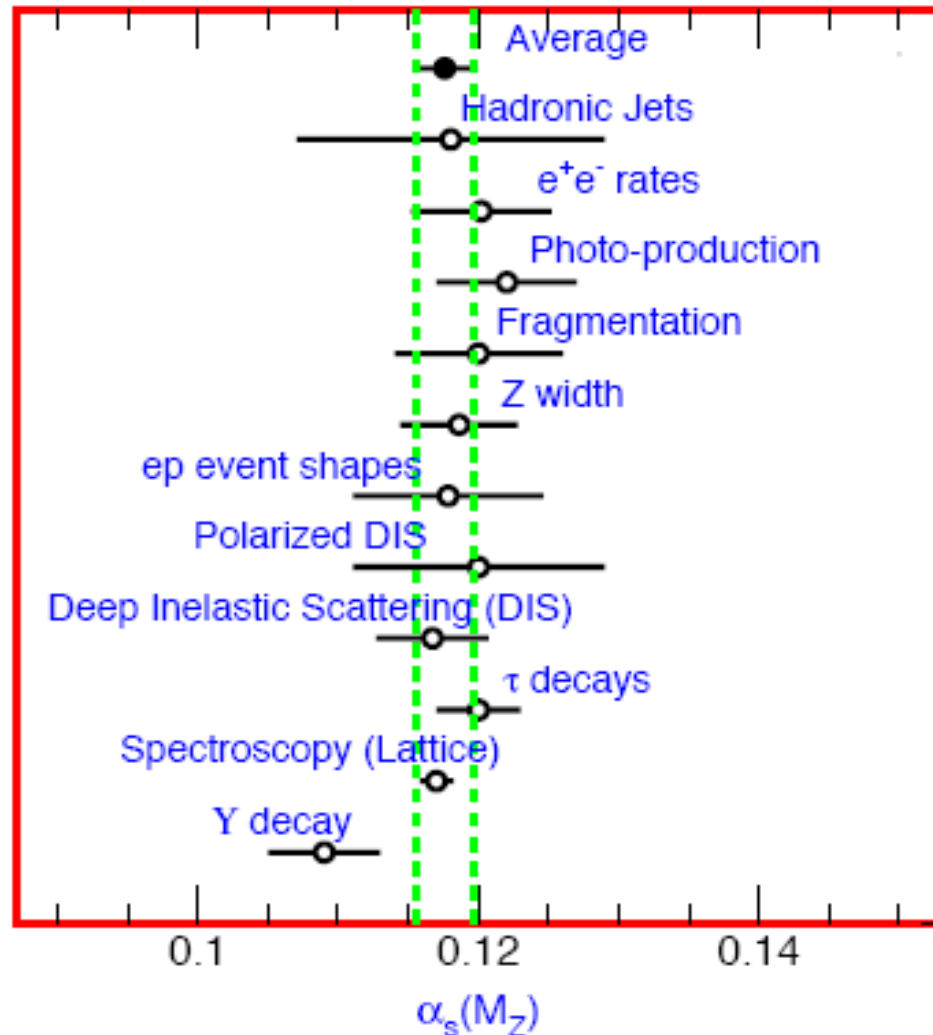
$$\alpha_s(M_Z) = \frac{\alpha_s(\mu_R)}{1 - \alpha_s(\mu_R)(b_0 + b_1\alpha_s(\mu_R)) \ln(\mu_R/M_Z)}$$

(2- and 3-loop RGE solutions are used in this analysis)

- In jet production: $\mu_r = \text{jet pT}$

Status of α_s measurements

From: 2008 Review of Particle Physics



Large uncertainty for entry from “Hadronic Jets”

→ Not very competitive with other relevant results
→ Can (and should) be improved!

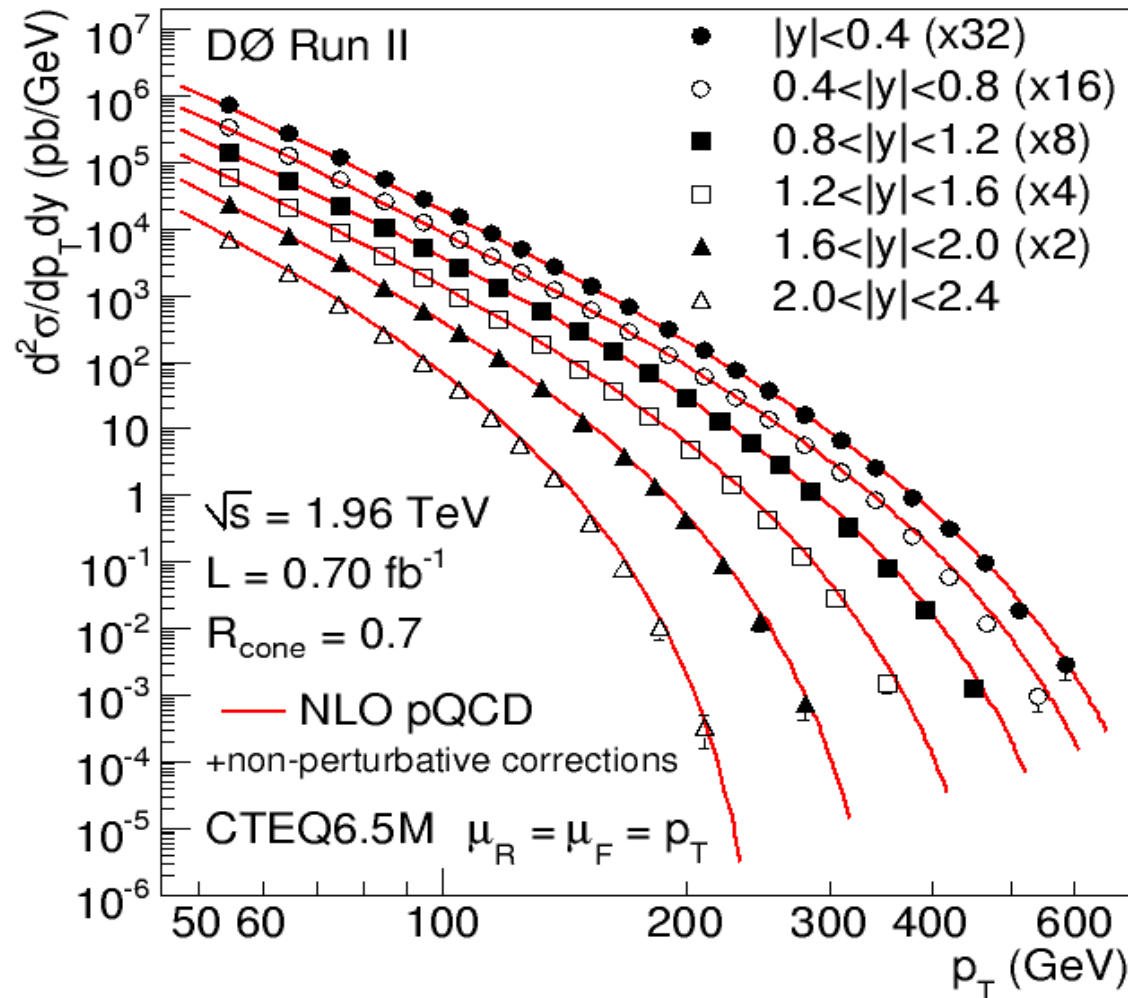
Now we have:

- More and better data
- Better theory

Figure 9.1: Summary of the value of $\alpha_s(M_Z)$ from various processes. The values shown indicate the process and the measured value of α_s extrapolated to $\mu = M_Z$. The error shown is the *total* error including theoretical uncertainties. The average quoted in this report which comes from these measurements is also shown. See text for discussion of errors.

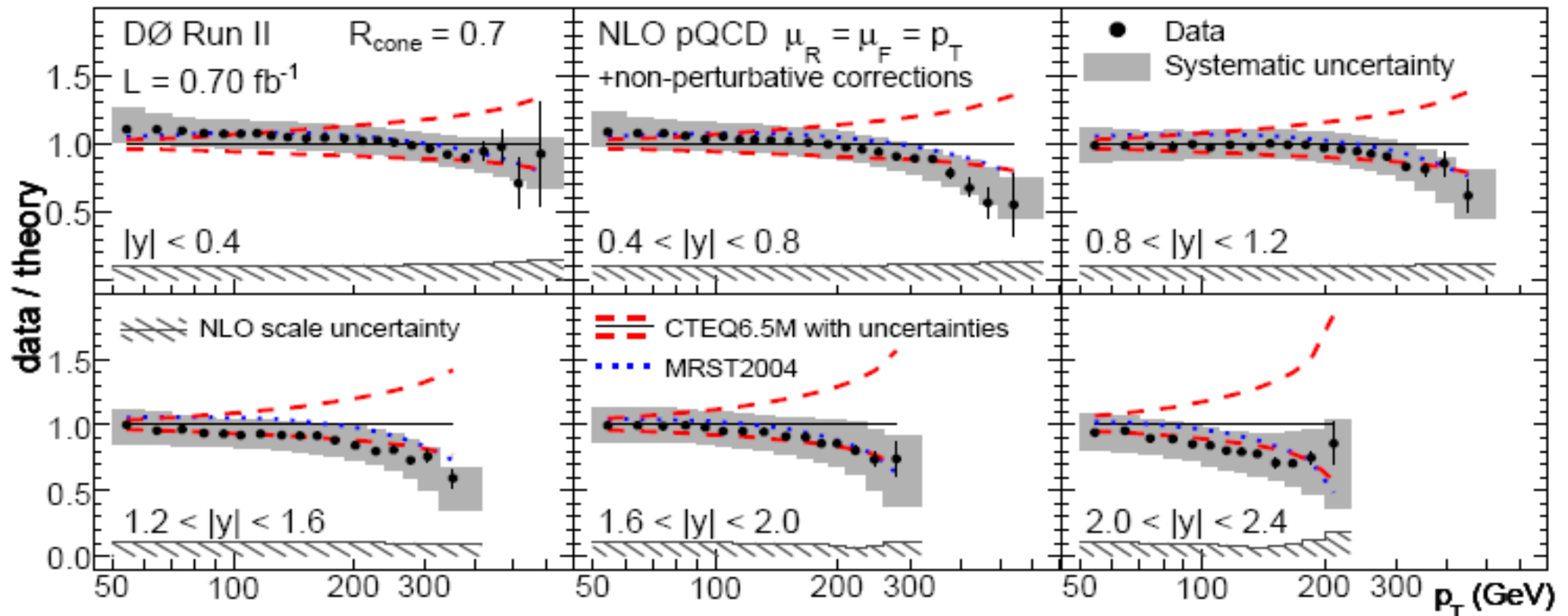
Run IIa Inclusive Jet Data (1)

D0 inclusive jet results: 110 cross section data points in six $|y|$ regions:
PRL 101, 062001 (2008)



Run IIa Inclusive Jet Data (2)

- The systematic errors are significantly reduced due to excellent results of Jet Energy Scale group
- Overall uncertainties allow now to better distinguish a preferred PDF set




Every single data point is sensitive to $\alpha_s(p_T)$

→ Sensitive to running of $\alpha_s(p_T)$

→ Combined fit (of **selected** data points): $\alpha_s(M_Z)$ result

Basic principle (naïve version)

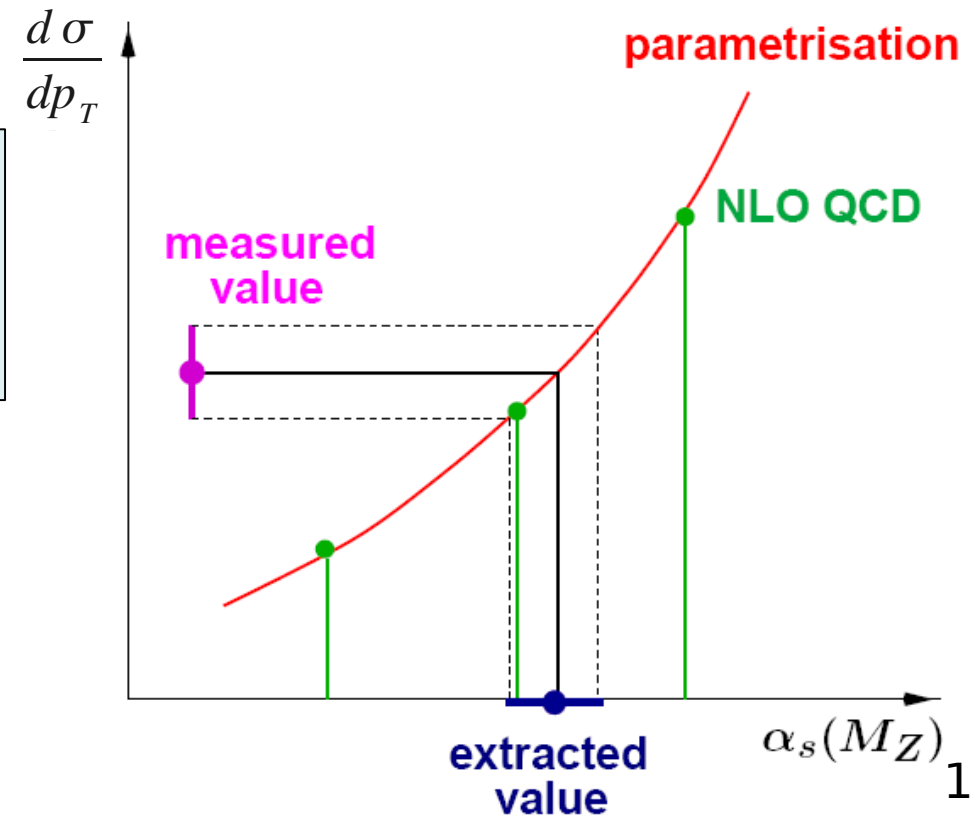
- Cross section formula:

$$\sigma_{\text{theory}}(\alpha_s) = \left(\sum_n \alpha_s^n c_n \right) \otimes f_1 \otimes f_2$$


- c_n : perturbative coefficients (\rightarrow pQCD matrix elements)
- f_1, f_2 : PDFs of colliding p, \bar{p}

Determine α_s from data:


- Vary α_s until σ_{theory} agrees with σ_{exper}
- ...for each single bin \rightarrow



α_s dependence of PDFs

- PDFs are always determined for a given value of $\alpha_s(M_z)$
→ PDF fit results depend on α_s

Naïve x-section formula must be modified to take α_s dependence of PDFs into account:

$$\sigma_{\text{theory}}(\alpha_s) = \left(\sum_n \alpha_s^n c_n \right) \otimes f_1(\alpha_s) \otimes f_2(\alpha_s)$$


Vary α_s in matrix elements **AND** in PDFs
until $\sigma_{\text{theory}}(\alpha_s) = \sigma_{\text{exper}}$

- Ideally need continuous α_s dependence of PDFs
- Requires: interpolation between cross section for PDFs with different $\alpha_s(M_z)$ values

α_s dependence of PDFs (2)

Interpolation must cover whole range of possible uncertainties

→ test interpolation over: $0.105 < \alpha_s(M_Z) < 0.130$

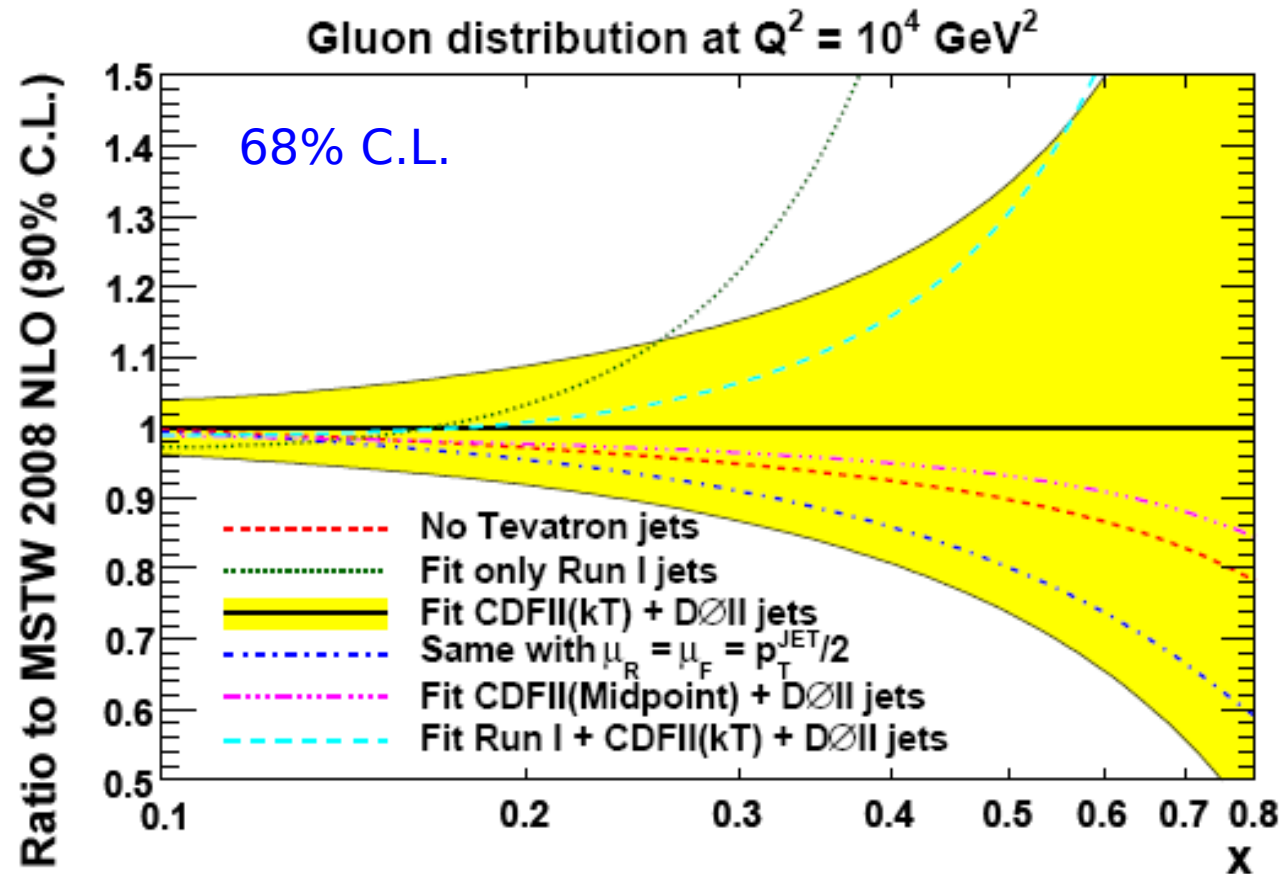
- MSTW2008 has **21** PDFs sets (NLO and NNLO!)
 - for α_s within 0.107-0.127 in 0.001 steps (→ 21 “nodes”)
 - use interpolation for points in between those 21
 - **used for the default results**
- CTEQ6.6 has **five** PDFs sets (NLO only)
 - for $\alpha_s(M_Z)=0.112, 0.114, 0.118, 0.122, 0.125$ (5 “nodes”)
 - **used for a comparison**

PDFs and input data (1)

- Tevatron RunII jet data have already been used in MSTW2008 PDF fits
 - only source of high- x gluon information
 - α_s extraction would be circular argument
 - PDFs uncertainties are correlated to experimental uncertainties (but correlation is not documented)
- **Restrict the data set used in the fit** to x -values where Tevatron jets are not the dominant source of information
- Somewhere up to $x = 0.2-0.3$ (see next slide)

PDFs and input data (2)

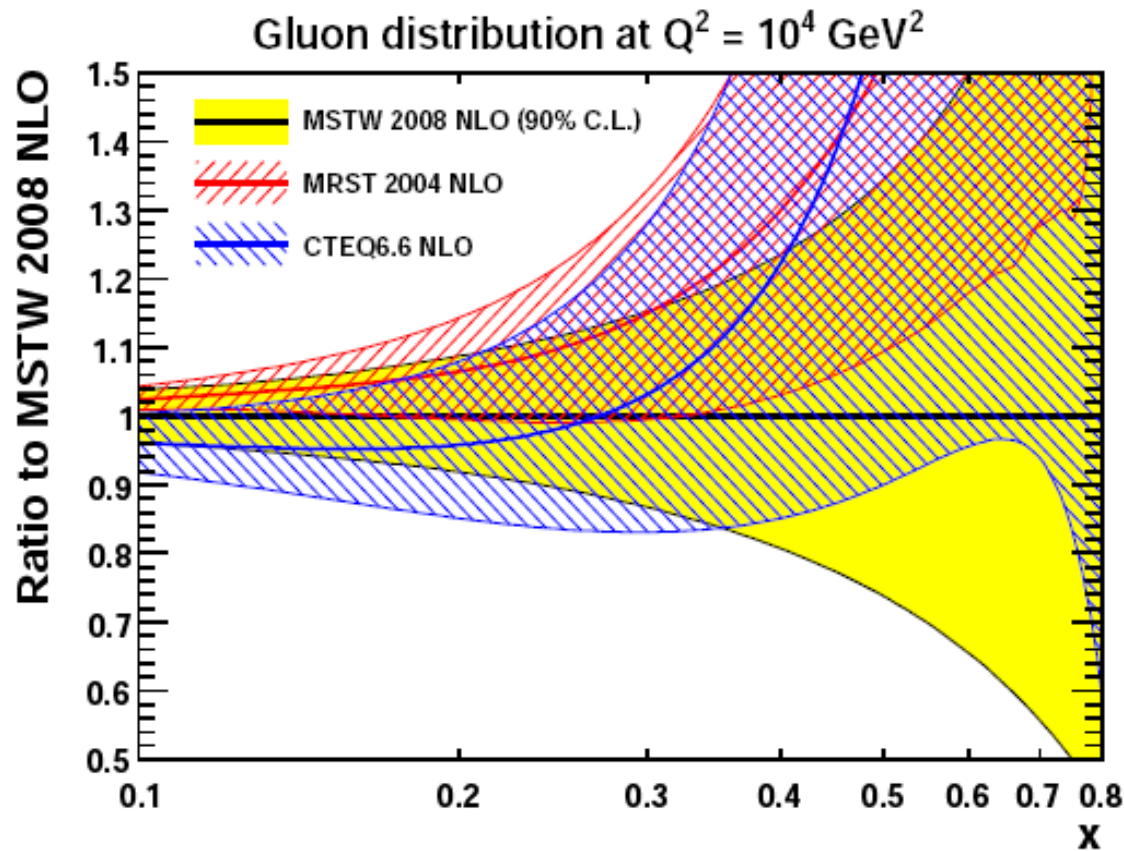
from MSTW2008 paper (arXiv:0901.0002 [hep-ph])



→ Tevatron jet data do not affect gluon PDF for $x < 0.2 - 0.3$

PDFs and input data (3)

from MSTW2008 paper



- CTEQ6.6 does not use Tevatron Run II jet data
- But MSTW2008 and CTEQ6.6 results are in agreement for $x < 0.3$

x-sensitivity?

Jet cross section has access to x-values of: (in LO kinematics)

$$x_a = x_T \frac{e^{y_1} + e^{y_2}}{2}, \quad x_b = x_T \frac{e^{-y_1} + e^{-y_2}}{2} \quad \text{with} \quad x_T = \frac{2 p_T}{\sqrt{s}}.$$

What is the x-value for a given incl. jet data point @(pT, |y|) ?

- Not completely constrained (unknown kinematics since we integrate over other jet)
- Construct 'test-variable' (treat as if other jet was at y=0):

$$x_{\text{test}} = x_T \cdot (e^{|y|} + 1)/2$$

- Apply cut on this test-variable to restrict accessible x-range
- Requirement **x-test < 0.15** removes most of the contributions with x>0.25
- 22 points are remaining (4 points for jet pT 50-60, ..., 1 point for 130-145 GeV)

Theory

Use **two alternative** theory predictions:

pQCD:

- **NLO + 2-loop threshold corrections** ('NLO + 2-loop')
(threshold corrections from Kidonakis/Owens)
- **NLO**

Uncertainties: scale dependence $\mu=p_T$ (+ x0.5 , x2.0)

PDFs:

- MSTW2008NNLO (for 'NLO+2-loop')
- MSTW2008NLO (for NLO)

Uncertainties: from 20 PDF eigenvectors (68%CL)

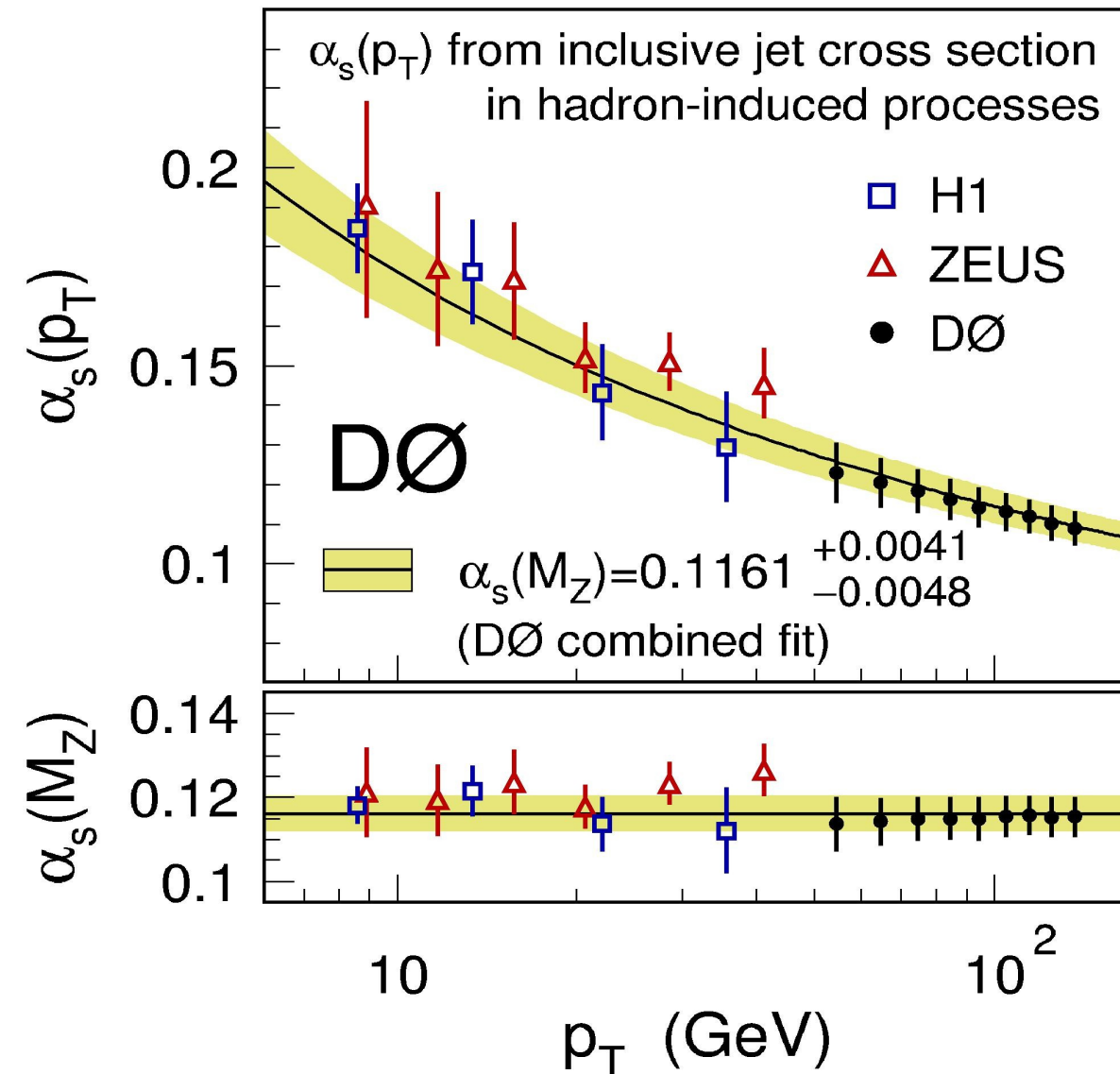
Non perturbative corrections: (hadronization / underlying events)

- from PYTHIA (as published with data)

Uncertainties: - half the size of the correction
- separately for hadronization and underlying events

Measurement of $\alpha_s(p_T)$

- Combine points in different $|y|$ regions at same p_T
→ Produce 9 $\alpha_s(p_T)$ points from selected 22 data points



Theory: NLO+2-loop threshold corrections

Compare to HERA results from H1 and ZEUS
→ consistency
→ our results extend p_T reach of HERA results to p_T range 50-145 GeV
→ α_s is running at the highest p_T measured so far!

Combined $\alpha_s(M_Z)$

Based on 22 inclusive jet data points with $x\text{-test} < 0.15$

Combined $\alpha_s(M_Z)$:

$$\alpha_s(M_Z) = 0.1161^{+0.0041}_{-0.0048}$$

$$= 0.1202^{+0.0072}_{-0.0059}$$

NLO + 2-loop threshold corrections

NLO

TABLE I: Central values and uncertainties due to different sources for the nine $\alpha_s(p_T)$ results and for the combined $\alpha_s(M_Z)$ result (bottom). All uncertainties are multiplied by a factor of 10^3 .

p_T range (GeV)	No. of data points	p_T (GeV)	$\alpha_s(p_T)$	total uncertainty	experimental uncorrelated	experimental correlated	non-perturb. correction	PDF uncertainty	$\mu_{r,f}$ variation
50 - 60	4	54.5	0.1229	$^{+7.6}_{-7.7}$	± 0.4	$^{+4.8}_{-4.9}$	$^{+5.8}_{-5.6}$	$^{+0.4}_{-0.6}$	$^{+1.0}_{-1.9}$
60 - 70	4	64.5	0.1204	$^{+6.2}_{-6.3}$	± 0.3	$^{+4.1}_{-4.3}$	$^{+4.5}_{-4.3}$	$^{+0.6}_{-0.5}$	$^{+1.3}_{-1.5}$
70 - 80	3	74.5	0.1184	$^{+5.6}_{-5.6}$	± 0.3	$^{+3.8}_{-3.9}$	$^{+4.0}_{-3.9}$	$^{+0.6}_{-0.6}$	$^{+1.0}_{-0.9}$
80 - 90	3	84.5	0.1163	$^{+5.1}_{-5.1}$	± 0.3	$^{+3.6}_{-3.7}$	$^{+3.5}_{-3.5}$	$^{+0.7}_{-0.7}$	$^{+0.9}_{-0.6}$
90 - 100	2	94.5	0.1142	$^{+5.1}_{-4.9}$	± 0.3	$^{+3.5}_{-3.6}$	$^{+3.5}_{-3.3}$	$^{+0.8}_{-0.8}$	$^{+1.1}_{-0.6}$
100 - 110	2	104.5	0.1131	$^{+4.7}_{-4.7}$	± 0.2	$^{+3.4}_{-3.5}$	$^{+3.1}_{-3.0}$	$^{+0.8}_{-0.8}$	$^{+1.1}_{-0.6}$
110 - 120	2	114.5	0.1121	$^{+4.2}_{-4.4}$	± 0.2	$^{+3.1}_{-3.3}$	$^{+2.5}_{-2.7}$	$^{+0.7}_{-0.8}$	$^{+1.2}_{-0.7}$
120 - 130	1	124.5	0.1102	$^{+4.4}_{-4.4}$	± 0.2	$^{+3.2}_{-3.4}$	$^{+2.6}_{-2.6}$	$^{+0.9}_{-0.9}$	$^{+1.4}_{-0.9}$
130 - 145	1	136.5	0.1090	$^{+4.2}_{-4.3}$	± 0.3	$^{+3.1}_{-3.4}$	$^{+2.3}_{-2.4}$	$^{+0.9}_{-0.9}$	$^{+1.5}_{-0.9}$
50 - 145	22	M_Z	0.1161	$^{+4.1}_{-4.8}$	± 0.1	$^{+3.4}_{-3.3}$	$^{+1.0}_{-1.6}$	$^{+1.1}_{-1.2}$	$^{+2.5}_{-2.9}$

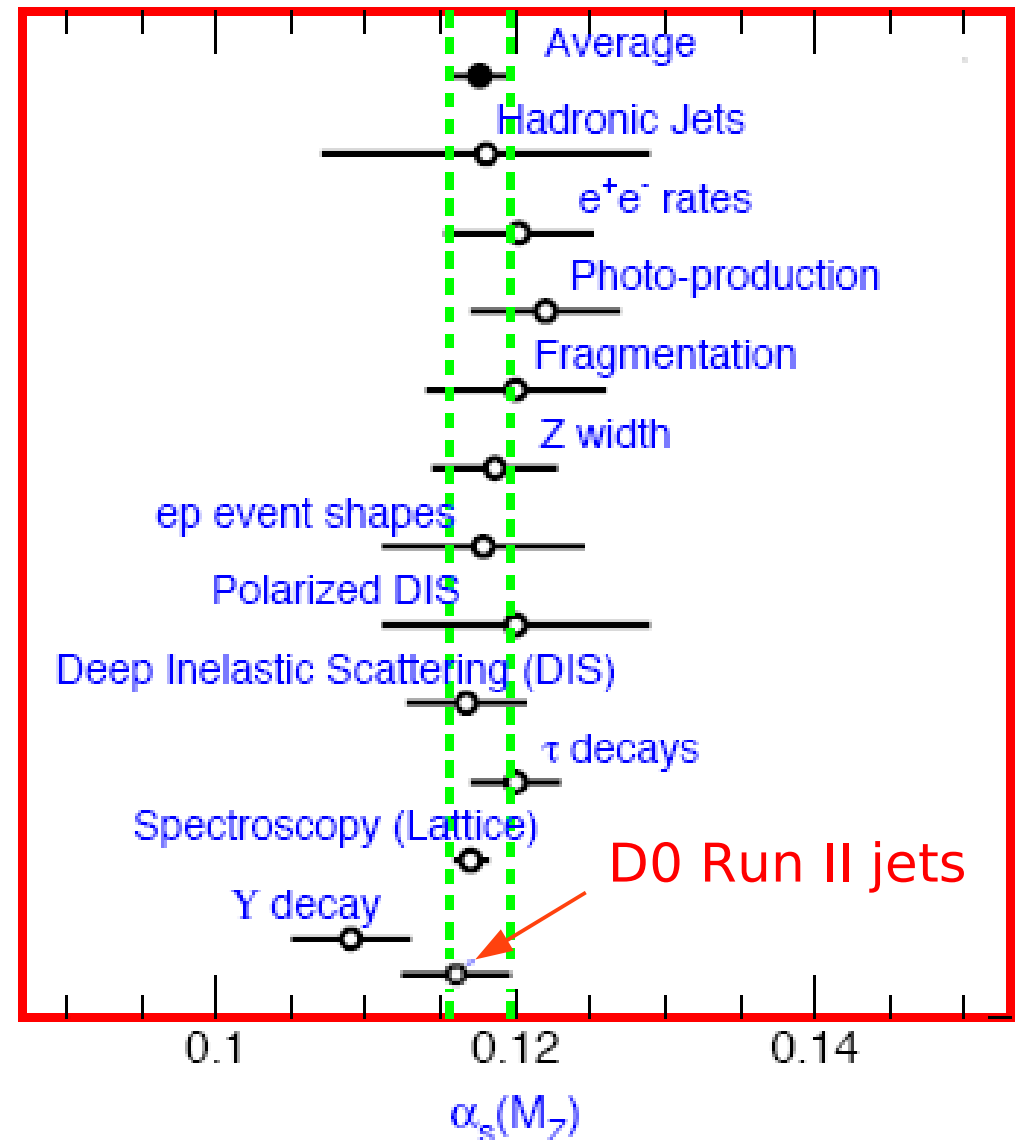
Main correlated uncertainties: JES, pT-resolution, luminosity

Summary on α_s

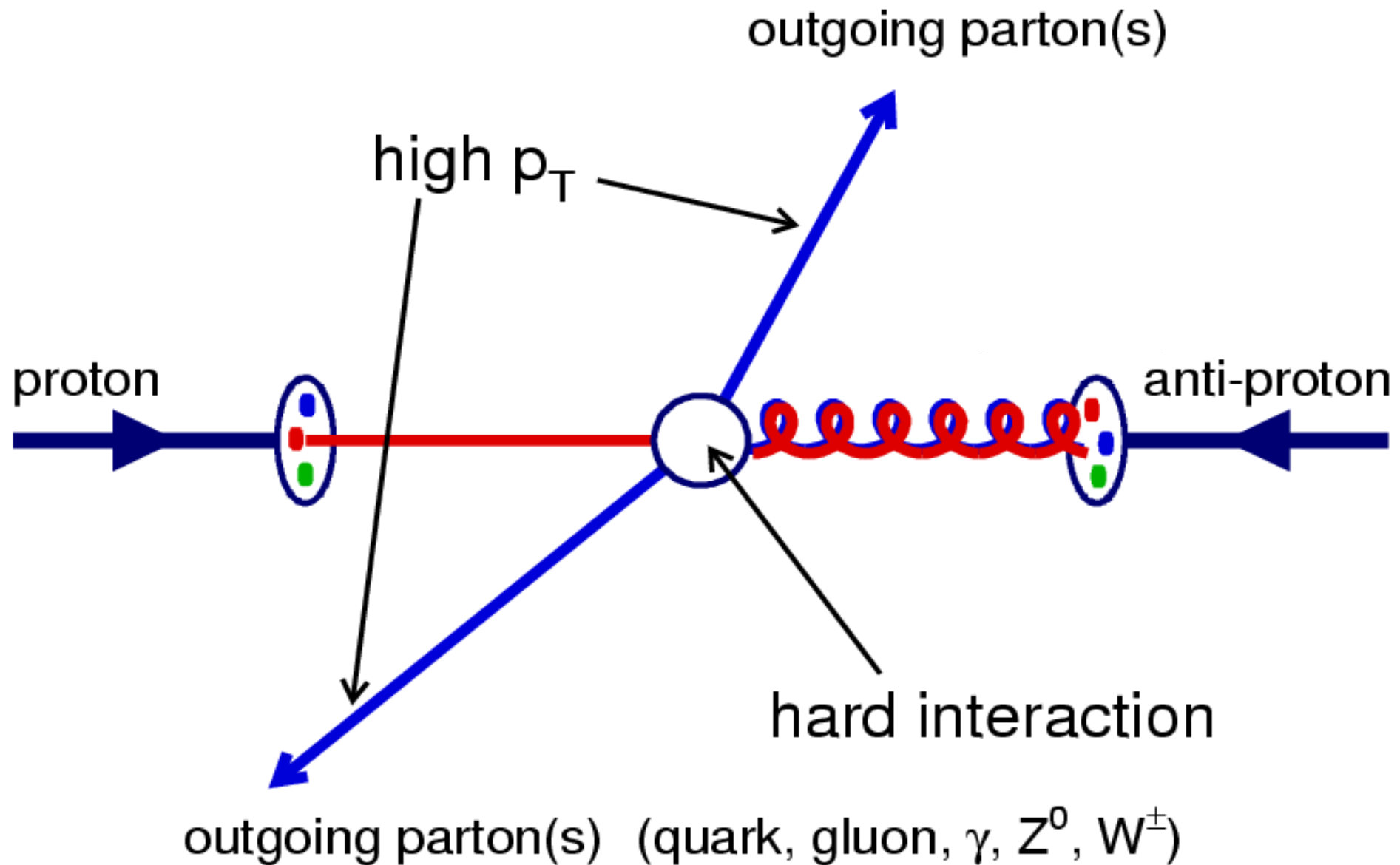
New α_s result from D0
inclusive jet pT cross sections

$$\alpha_s(M_Z) = 0.1161^{+0.0041}_{-0.0048}$$

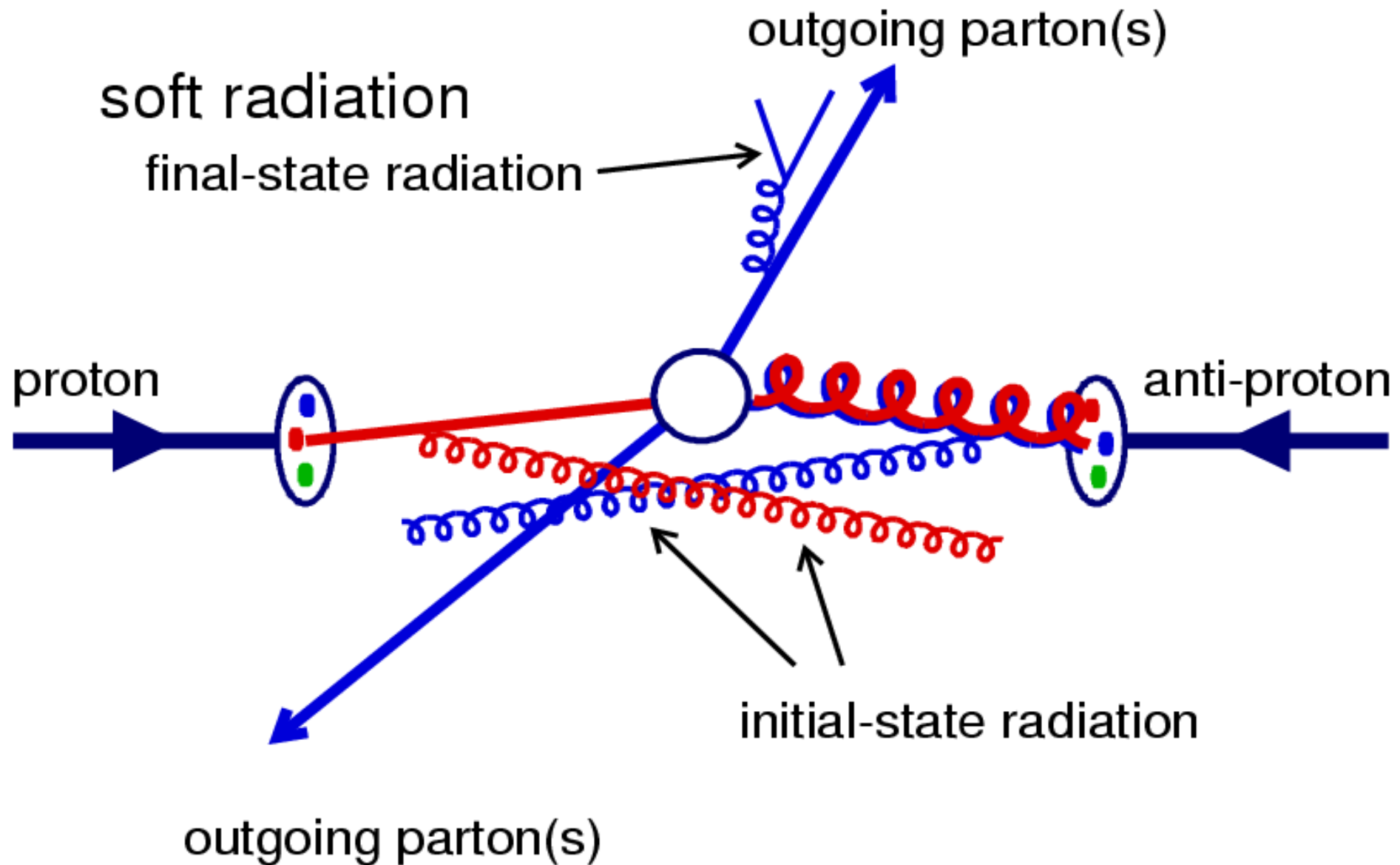
- The only Run II result on α_s
- Improvement by about factor 3 as compared with Run I
- Comparable precision with HERA jets (0.1189 ± 0.0032)
- Accepted by PRD RC ([arXiv.org:0911.2710](https://arxiv.org/abs/0911.2710) [hep-ex])



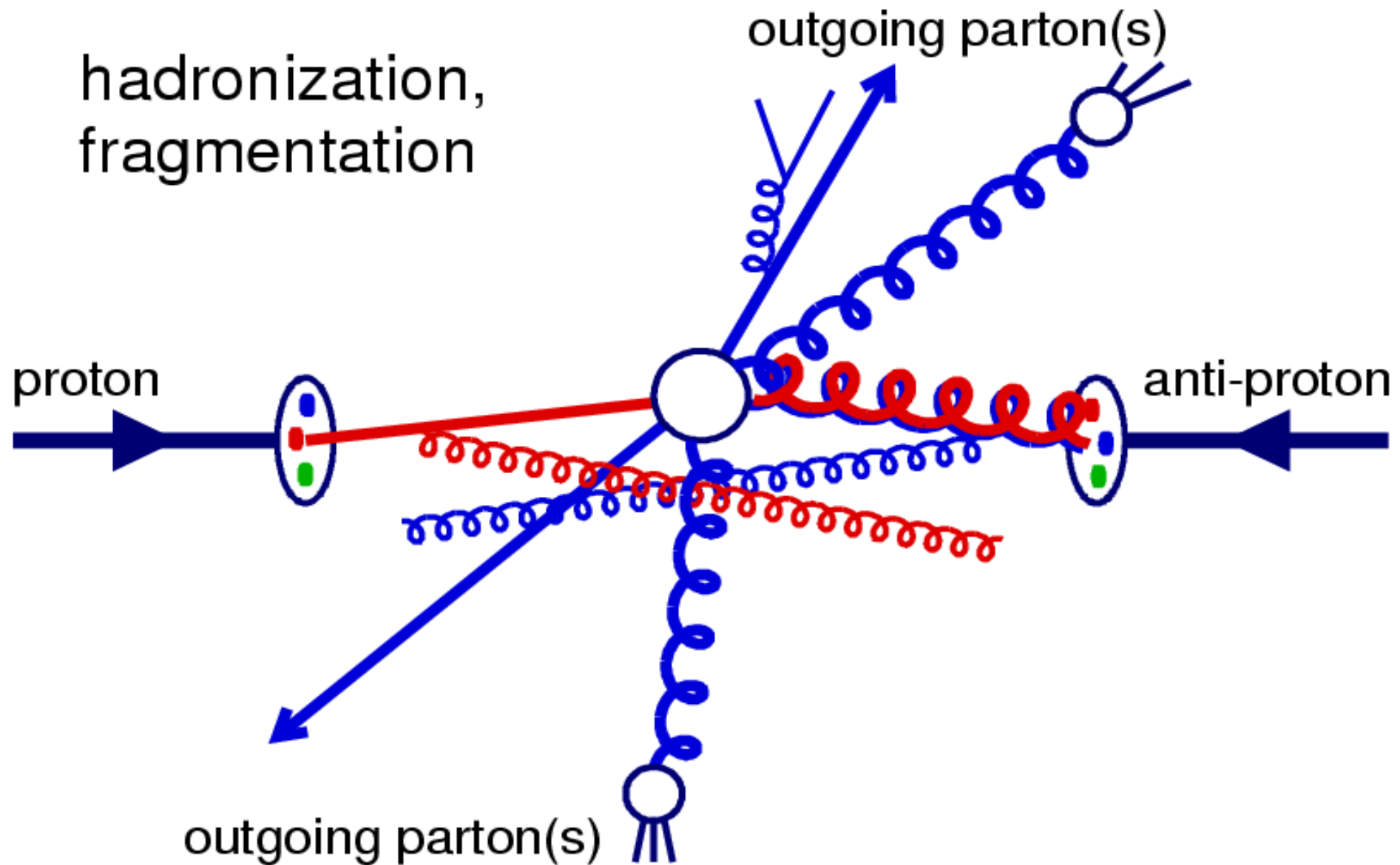
Hadron-Hadron Collision



Hadron-Hadron Collision

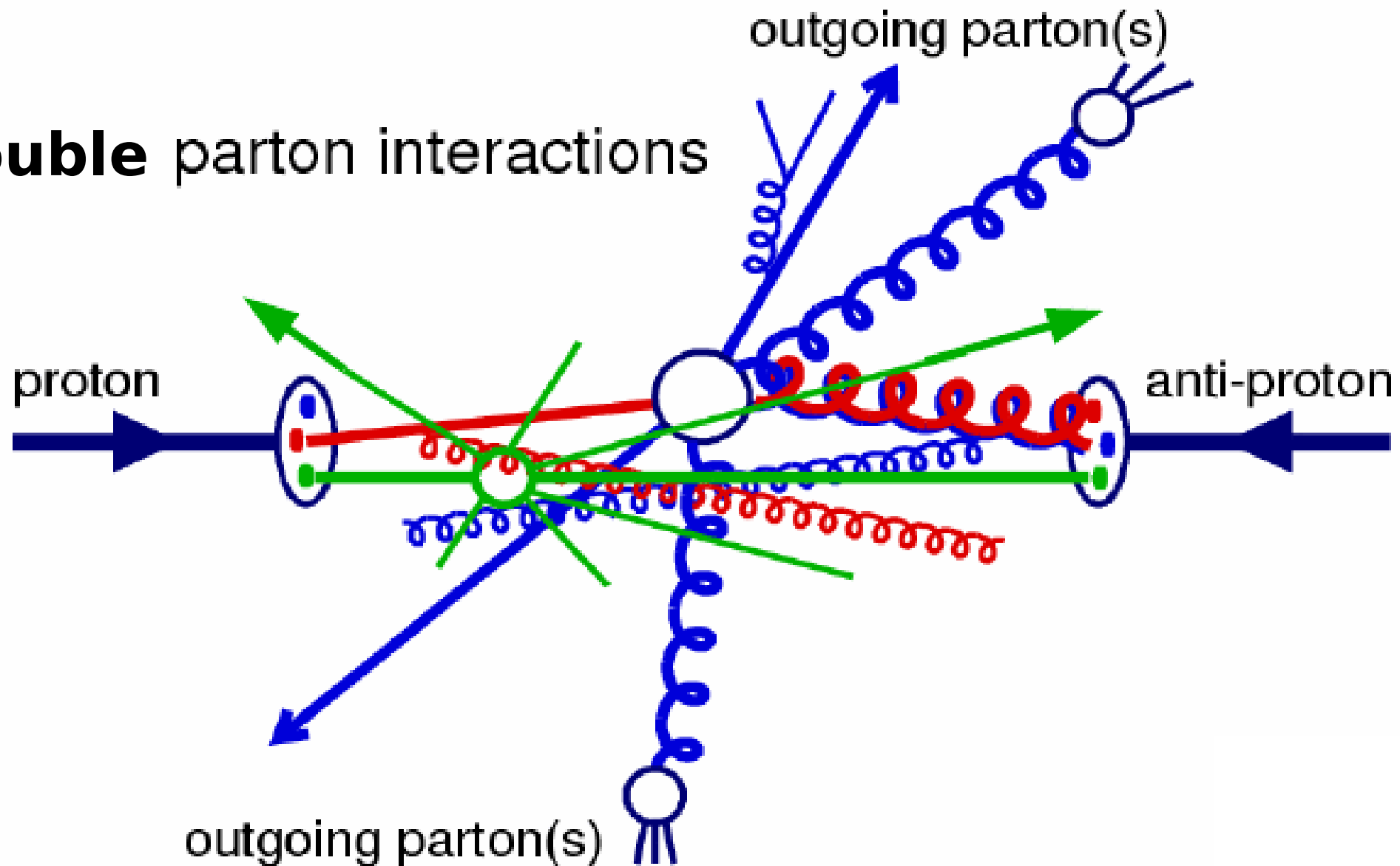


Hadron-Hadron Collision



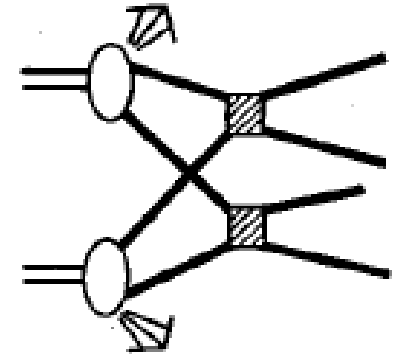
Hadron-Hadron Collision: from Single to Double parton interactions

Double parton interactions



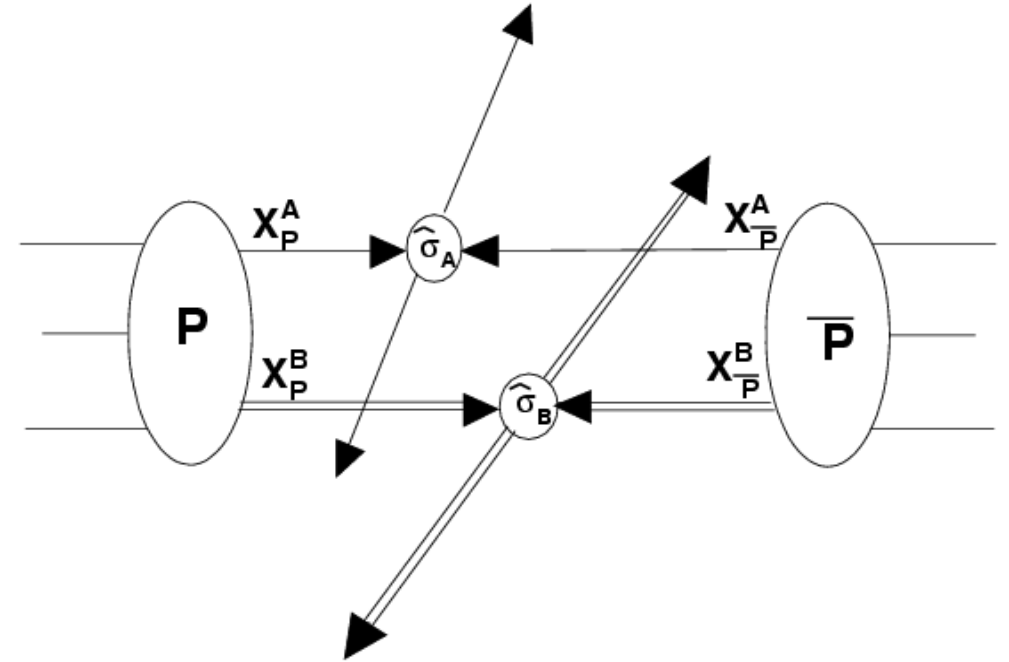
Double Parton Interactions in $\gamma+3$ jets events

- Motivations
- Event topology
- Discriminating variables
- Fraction of double parton events
- Effective cross-section measurement
- Conclusion



Double parton and effective cross sections

$$\sigma_{DP} = \frac{\sigma_A \sigma_B}{\sigma_{eff}}$$



σ_{DP} - double parton cross section for processes A and B

σ_{eff} - factor characterizing size of effective interaction region

→ contains information on the spatial distribution of partons.

Uniform: σ_{eff} is large and σ_{DP} is small

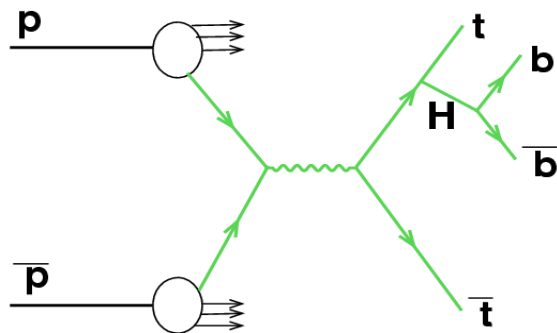
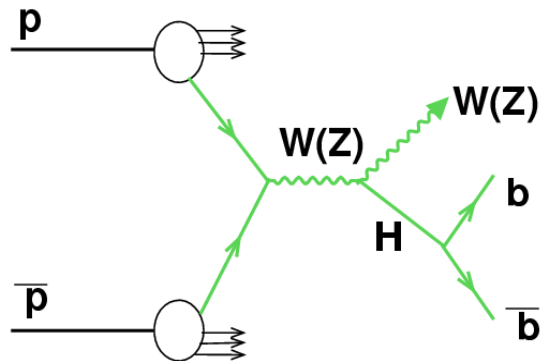
Clumpy: σ_{eff} is small and σ_{DP} is large

→ Needed for precise estimates of background to many rare processes (especially with multi-jet final state)

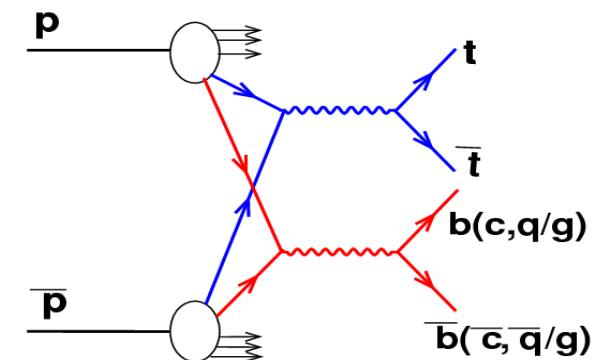
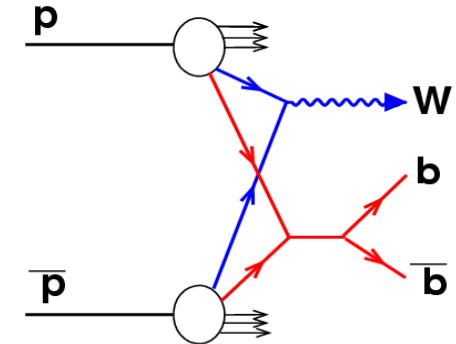
→ Should be measured in experiment !!

Double Parton events as a background to Higgs production

Signal



Double Parton background



- Many Higgs production channel can be mimicked by Double Parton event!
 - Some of them can be significant even after signal selections.
 - Dedicated cuts are required to increase sensitivity to the Higgs signal (same is true for many other rare processes)!
- => see example of possible variables below (and also 0911.5348[hep-ph])

Previous Double Parton measurements

	\sqrt{s} (GeV)	final state	p_T^{min} (GeV/c)	η range	Result
AFS, 1986	63	4jets	$p_T^{jet} > 4$	$ \eta^{jet} < 1$	$\sigma_{eff} \sim 5$ mb
UA2, 1991	630	4jets	$p_T^{jet} > 15$	$ \eta^{jet} < 2$	$\sigma_{eff} > 8.3$ mb (95% C.L.)
CDF, 1993	1800	4jets	$p_T^{jet} > 25$	$ \eta^{jet} < 3.5$	$\sigma_{eff} = 12.1_{-5.4}^{+10.7}$ mb
CDF, 1997	1800	$\gamma + 3jets$	$p_T^{jet} > 6$	$ \eta^{jet} < 3.5$	$\sigma_{eff} = 14.5 \pm 1.7_{-2.3}^{+1.7}$ mb
			$p_T^\gamma > 16$	$ \eta^\gamma < 0.9$	

CDF 1997: photon+3jet events, **data-driven method**:

To extract σ_{eff} : use of rates of events with Double Interaction (two separate $p \bar{p}$ collisions) and rates of Double Parton events from a single $p \bar{p}$ collision.

\Rightarrow reduce dependence on MC and NLO QCD theory predictions.

Measurement of σ_{eff}

For two hard scattering events:

$$P_{DI} = 2 \left(\frac{\sigma^{\gamma j}}{\sigma_{\text{hard}}} \right) \left(\frac{\sigma^{jj}}{\sigma_{\text{hard}}} \right)$$

The number of Double Interaction events:

$$N_{DI} = 2 \frac{\sigma^{\gamma j}}{\sigma_{\text{hard}}} \frac{\sigma^{jj}}{\sigma_{\text{hard}}} N_C(2) A_{DI} \epsilon_{DI} \epsilon_{2\text{vtx}}$$

For one hard interaction:

$$P_{DP} = \left(\frac{\sigma^{\gamma j}}{\sigma_{\text{hard}}} \right) \left(\frac{\sigma^{jj}}{\sigma_{\text{eff}}} \right)$$

Then the number of Double Parton events:

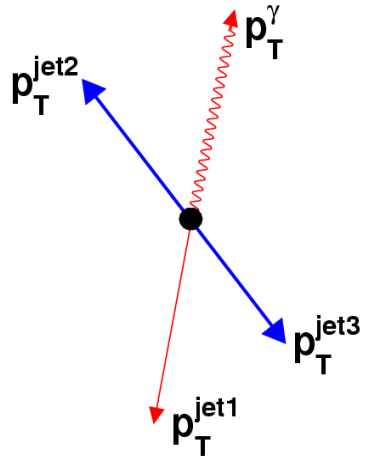
$$N_{DP} = \frac{\sigma^{\gamma j}}{\sigma_{\text{hard}}} \frac{\sigma^{jj}}{\sigma_{\text{eff}}} N_C(1) A_{DP} \epsilon_{DP} \epsilon_{1\text{vtx}}$$

Therefore one can extract:

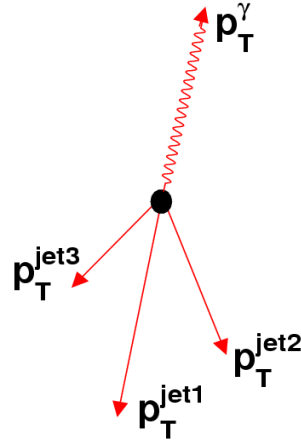
$$\sigma_{\text{eff}} = \frac{N_{DI}}{N_{DP}} \frac{N_C(1)}{2N_C(2)} \frac{A_{DP}}{A_{DI}} \frac{\epsilon_{DP}}{\epsilon_{DI}} \frac{\epsilon_{1\text{vtx}}}{\epsilon_{2\text{vtx}}} \sigma_{\text{hard}}$$

$\gamma+3$ jets events topology: Double Parton and Double Interaction events

DP



SP



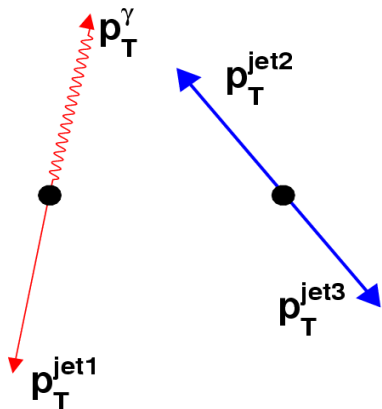
Signal: Double Parton (DP) production:

1st parton process produces γ -jet pair, while 2nd process produces dijet pair.

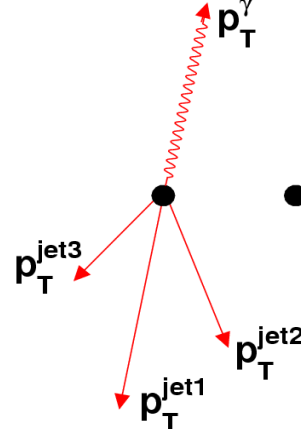
Background: Single Parton (SP) production:

single hard γ -jet scattering with 2 radiation jets in 1 vertex events.

DI



SP



Background: Single Parton (SP) production:

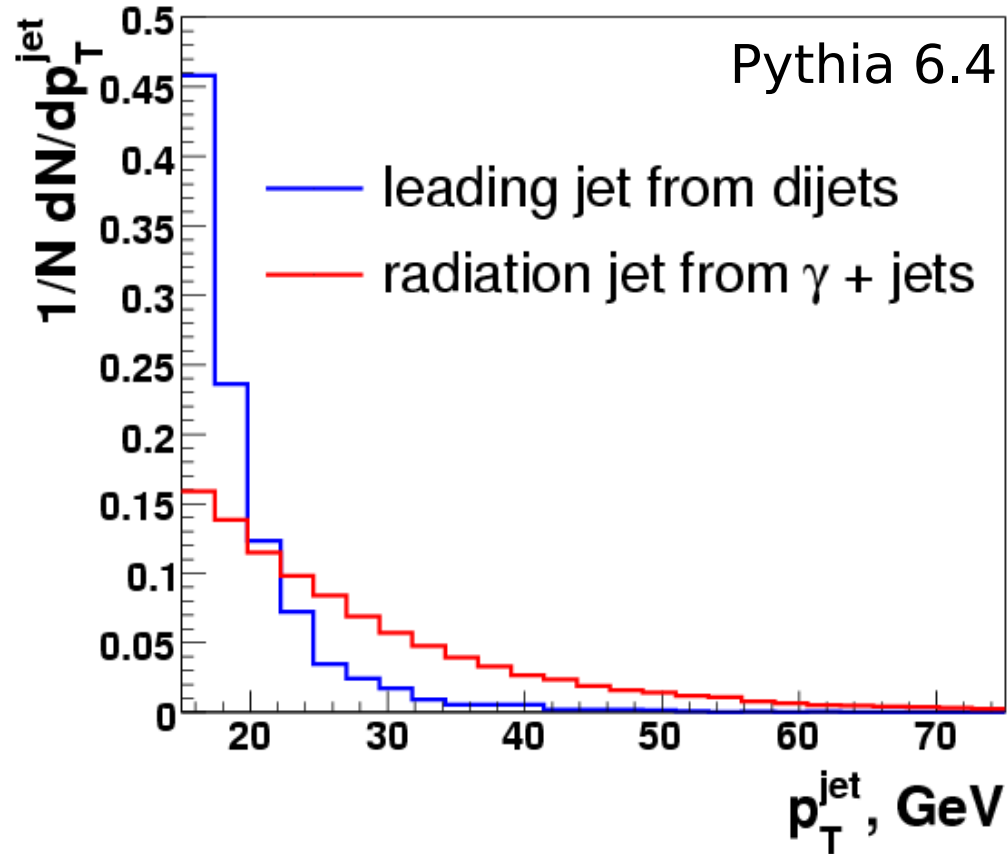
single hard γ -jet scattering in one vertex with 2 radiation jets and soft unclustered energy in the 2nd vertex.

Signal: Double Interaction (DI) production:

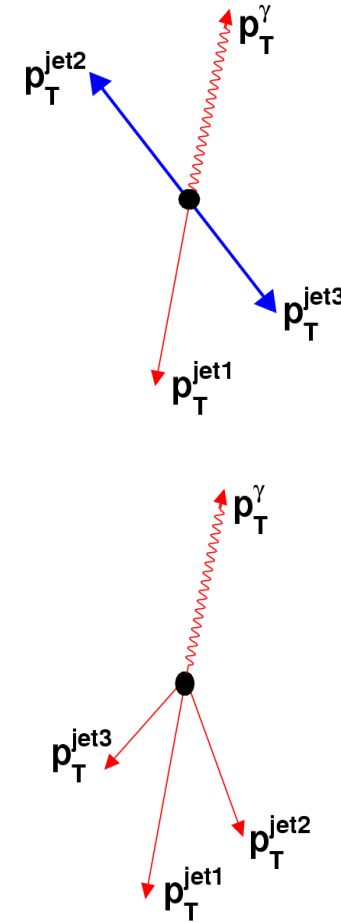
two separate collisions within the same beam crossing, producing γ -jet and dijet pairs.

Motivation for jet pT binning

Jet PT: jet from **dijets** vs. **radiation** jet from γ +jet events



$$\sim 1/p_T^4$$
$$\sim 1/p_T^2$$



- Jet pT from dijets falls much faster than that for radiation jets, i.e.
 - Fraction of dijet (Double Parton) events should drop with increasing jet PT
 - => Measurement is done in the three bins of 2nd jet pT: 15-20, 20-25, 25-30 GeV

Double Parton interaction model

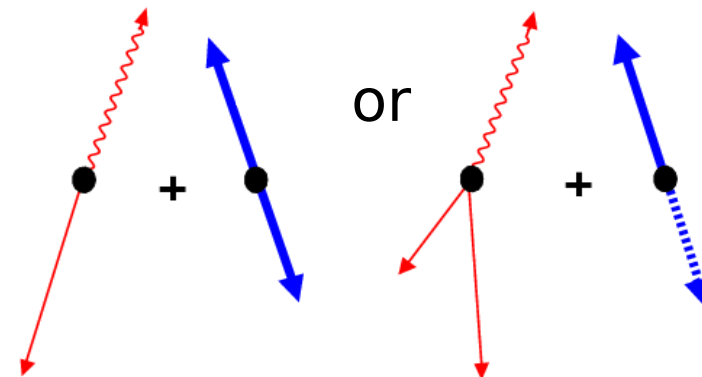
Built from D0 data. Samples:

A: photon + ≥ 1 jet from γ +jets data events:

- 1-vertex events
- photon p_T : 60-80 GeV
- leading jet $p_T > 25$ GeV, $|\eta| < 3.0$.

B: ≥ 1 jets from MinBias events:

- 1-vertex events
- jets with p_T 's recalculated to the primary vertex of sample A have $p_T > 15$ GeV and $|\eta| < 3.0$.



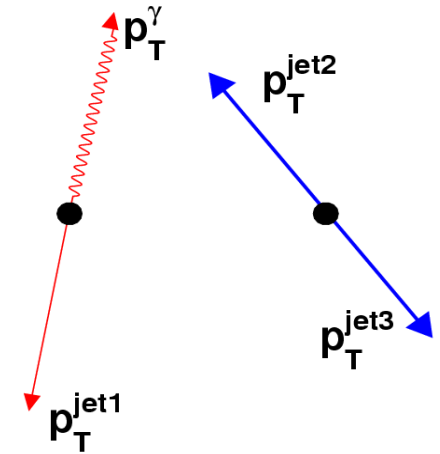
- ▶ **A** & **B** samples have been (randomly) mixed with jets p_T re-ordering
- ▶ Events should satisfy photon+ ≥ 3 jets requirement.
- ▶ $\Delta R(\text{photon}, \text{jet1}, \text{jet2}, \text{jet3}) > 0.7$

⇒ Two scatterings are independent by construction

Double $p\bar{p}$ Interaction model

Built from D0 data by analogy to Double Parton model with the only difference: ingredient events (γ +jets and dijets) are 2-vertex events.

In case of 2 jets, both jets are required to originate from the same vertex using jet track information.



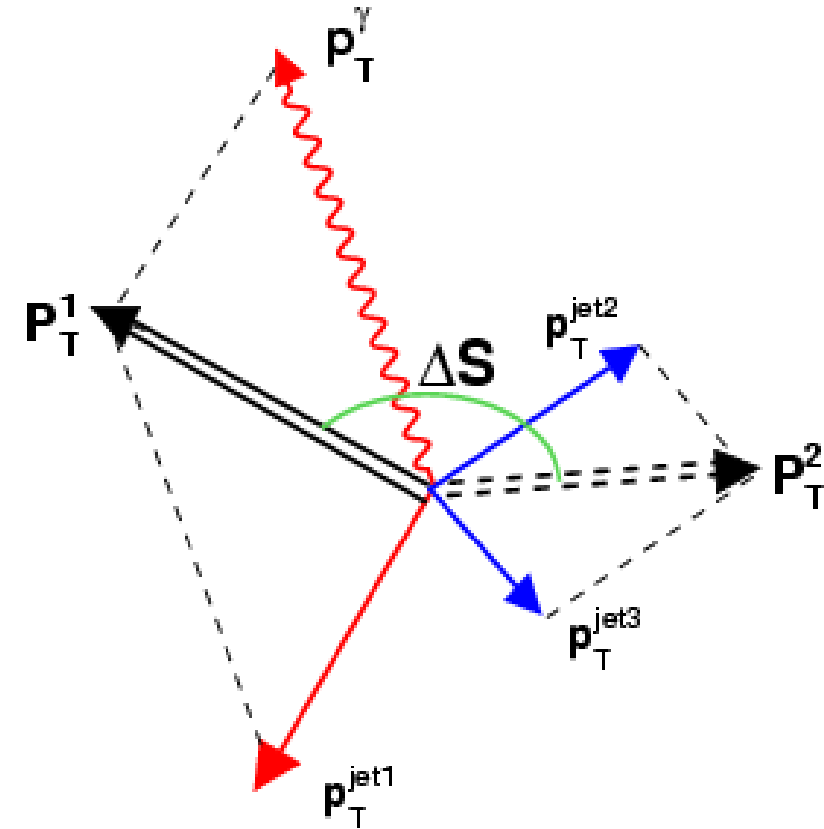
⇒ Main difference of Double Parton and Double $p\bar{p}$ Interaction signal events and corresponding SP backgrounds: different amount of soft unclustered energy in 1-vertex vs. 2-vertex events
→ different photon and jet ID efficiencies.

Discriminating variables

$$\Delta S = \Delta\phi(p_T^{\gamma, \text{jet}}, p_T^{\text{jet}_i, \text{jet}_k})$$

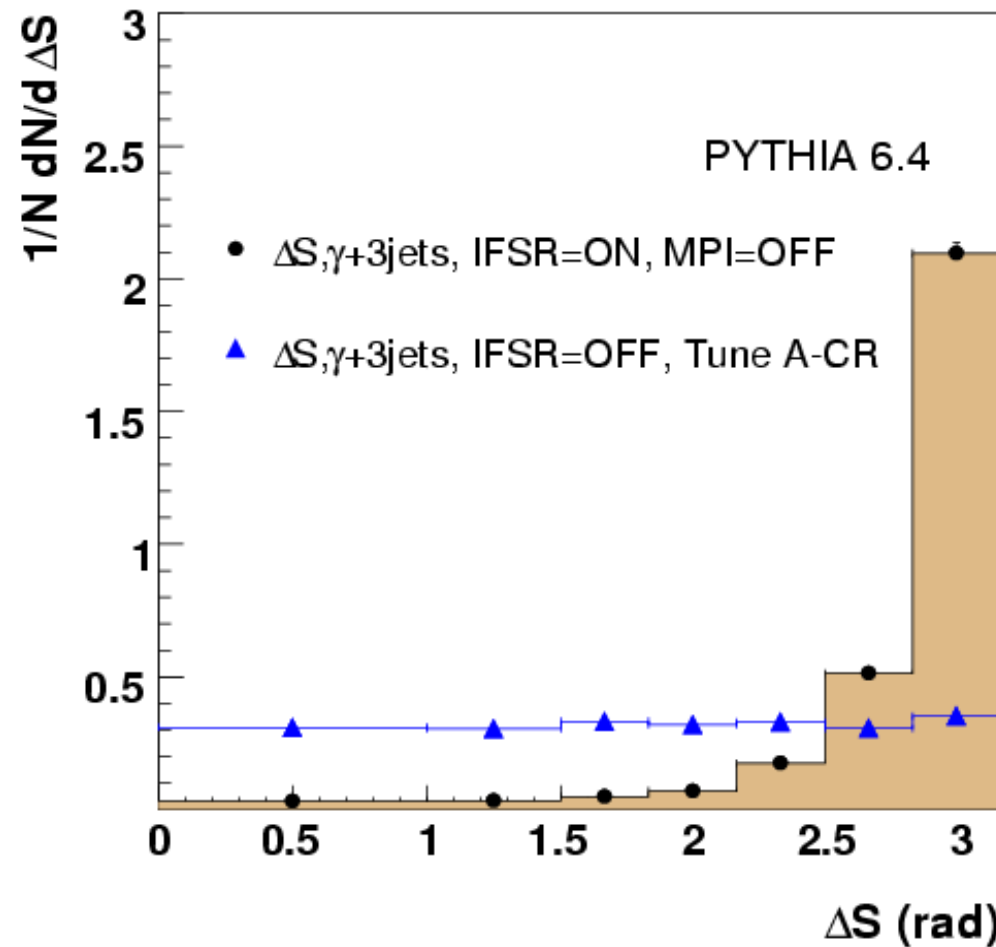
- ▶ $\Delta\phi$ angle between two best pT-balancing pairs →
- ▶ The pairs should correspond to a minimum S value:

$$S_\phi = \frac{1}{\sqrt{2}} \sqrt{\left(\frac{\Delta\phi(\gamma, i)}{\delta\phi(\gamma, i)}\right)^2 + \left(\frac{\Delta\phi(j, k)}{\delta\phi(j, k)}\right)^2}$$
$$S_{p_T} = \frac{1}{\sqrt{2}} \sqrt{\left(\frac{|\vec{P}_T(\gamma, i)|}{\delta P_T(\gamma, i)}\right)^2 + \left(\frac{|\vec{P}_T(j, k)|}{\delta P_T(j, k)}\right)^2}$$



In the signal sample most likely (>94%) S-variables are minimized by pairing photon with the leading jet.

ΔS distribution for $\gamma+3\text{jets}$ events from Single Parton scattering



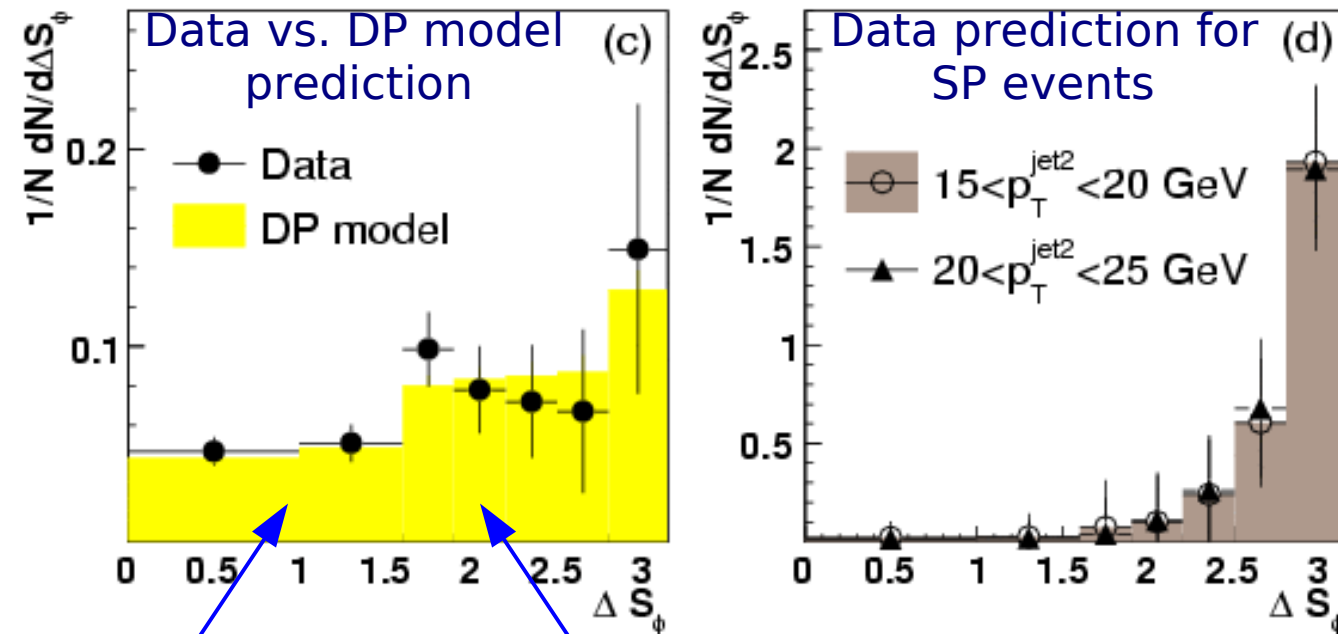
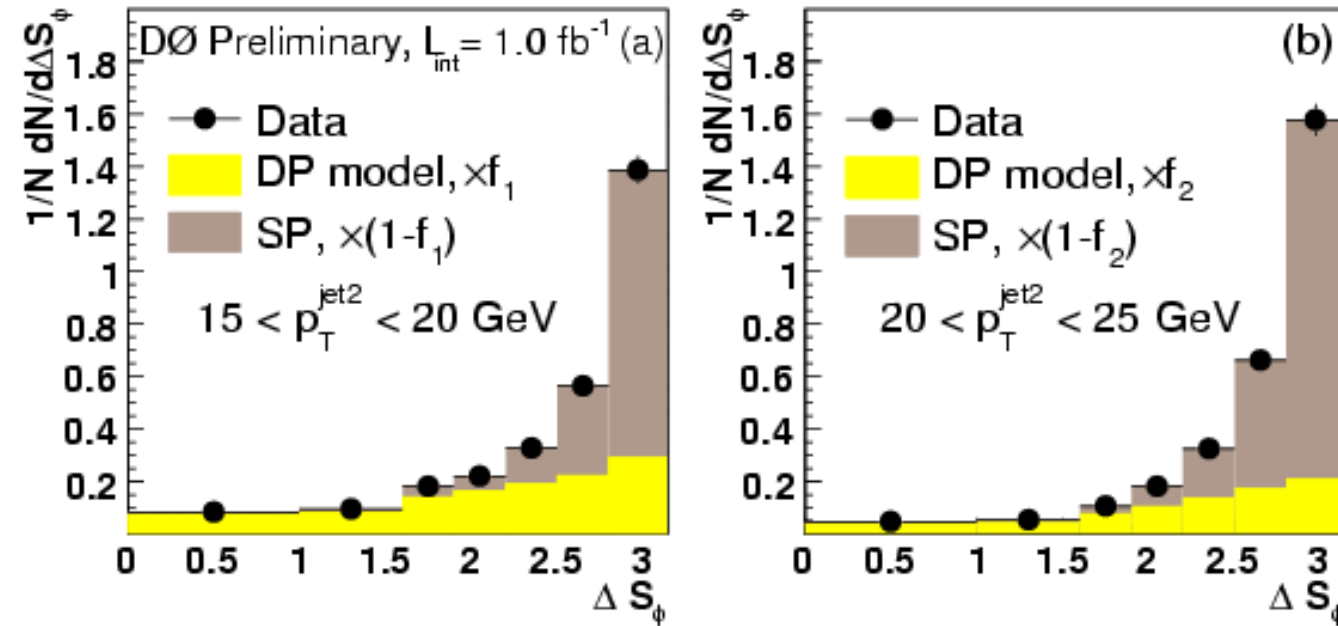
→ For “ $\gamma+3\text{jets}$ ” events from Single Parton scattering we expect ΔS to peak at π , while it should be flat for “ideal” Double Parton interaction (2nd and 3rd jets are from dijet production).

The two datasets method

Dataset (a): 2nd jet pT: 15-20 GeV

Dataset (b): 2nd jet pT: 20-25 GeV

✓ Fraction of Double Parton in bin 15-20 GeV (f_1) is the only unknown
→ get from minimization.

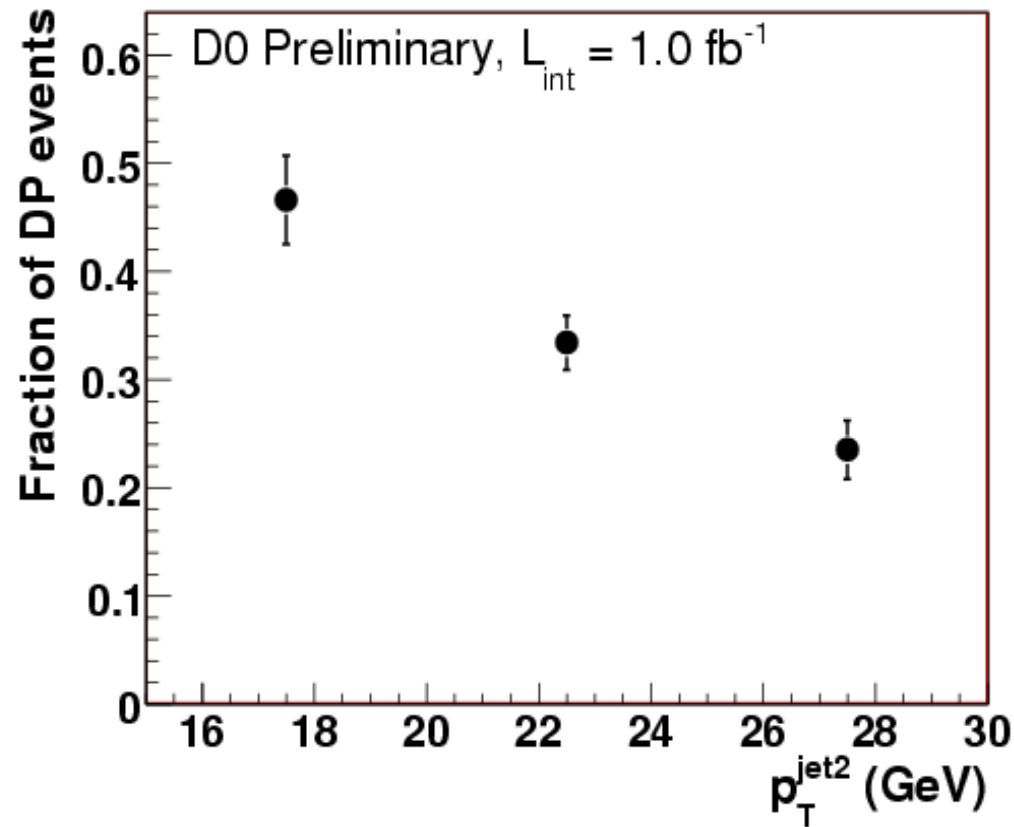


✓ Good agreement of the ΔS Single Parton distribution extracted in data and in MC (see previous slide)
→ another confirmation for the found DP fractions.

Data are corrected for the DP fractions

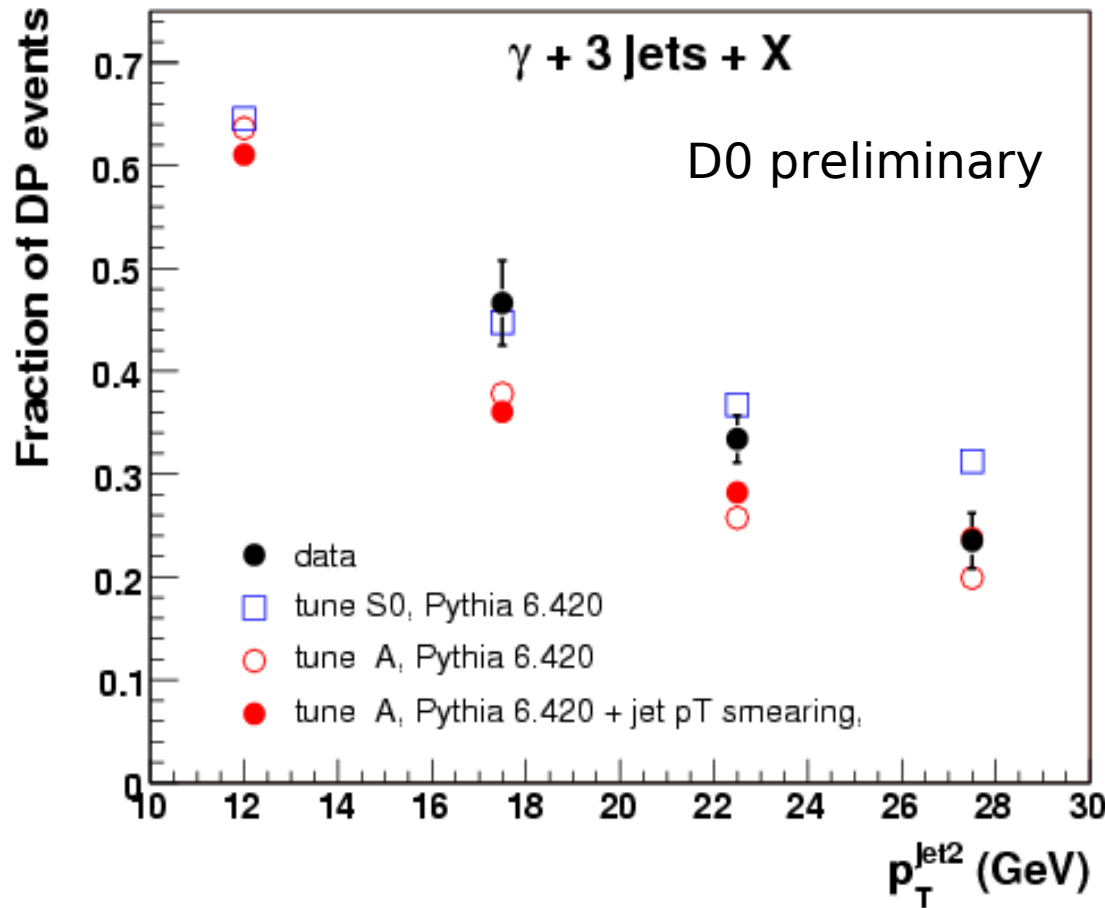
✓ Good agreement of Data and DP model

Fractions of Double Parton events



Fractions drop from $\sim 46\text{-}48\%$ at 2^{nd} jet $15 < p_T < 20$ GeV to $\sim 22\text{-}23\%$ at 2^{nd} jet $25 < p_T < 30$ GeV with relative uncertainties $\sim 7\text{-}12\%$.

Fractions of Double Parton events : MPI models and D0 data

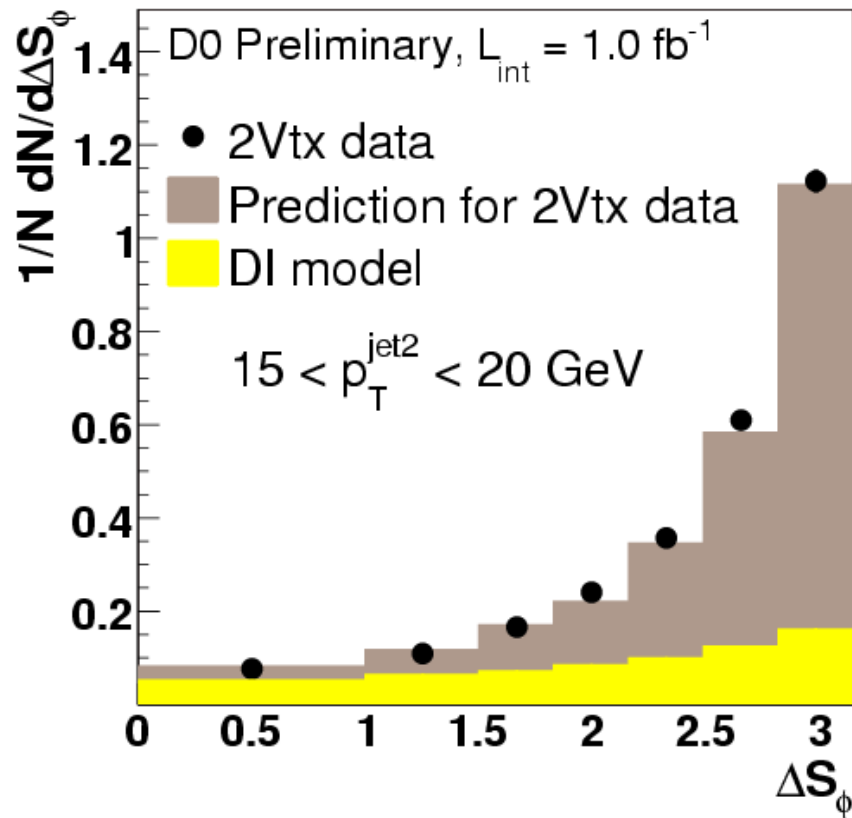


- Pythia MPI tunes A and S0 are considered.
- Data are in between the model predictions.
- Results are preliminary: data should be corrected to the particle level.
- Will be done later to find the best MPI Tune

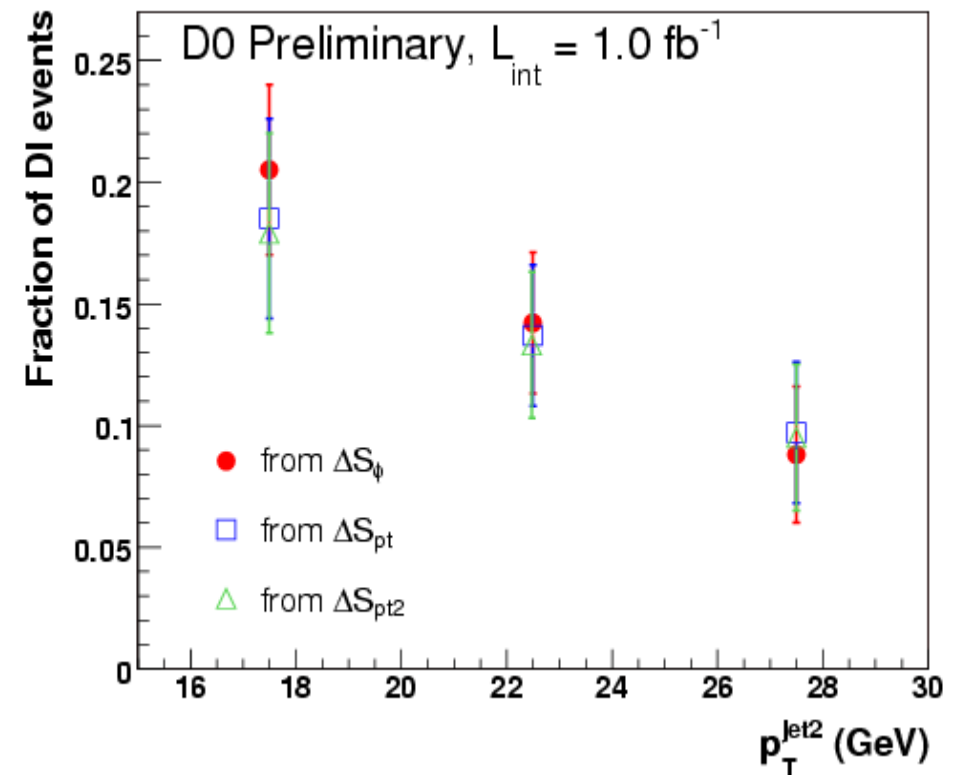
Fractions of Double $p\bar{p}$ Interactions (DI) events

To calculate σ_{eff} , we also need $N_{\text{DI}} = f_{\text{DI}} N_{2\text{vtx}}$.

→ use ΔS shapes and get f_{DI} by fitting DI signal and background distributions to 2-vertex data



Total sum of DI signal+bkgd, weighted with DI fractions, is in agreement with data



Main uncertainties in DI fractions are from building DI signal and background models

Calculation of $N_c(n)$ and σ_{hard}

Total numbers of events with 1 and 2 hard $p\bar{p}$ collisions, $N_c(1)$ and $N_c(2)$, are calculated from the expected average number of hard interactions at a given instantaneous luminosity L_{inst} :

$$\bar{n} = (L_{\text{inst}} / f_0) \sigma_{\text{hard}}$$

using Poisson statistics.

f_0 is a frequency of the beam crossings at the Tevatron in RunII.

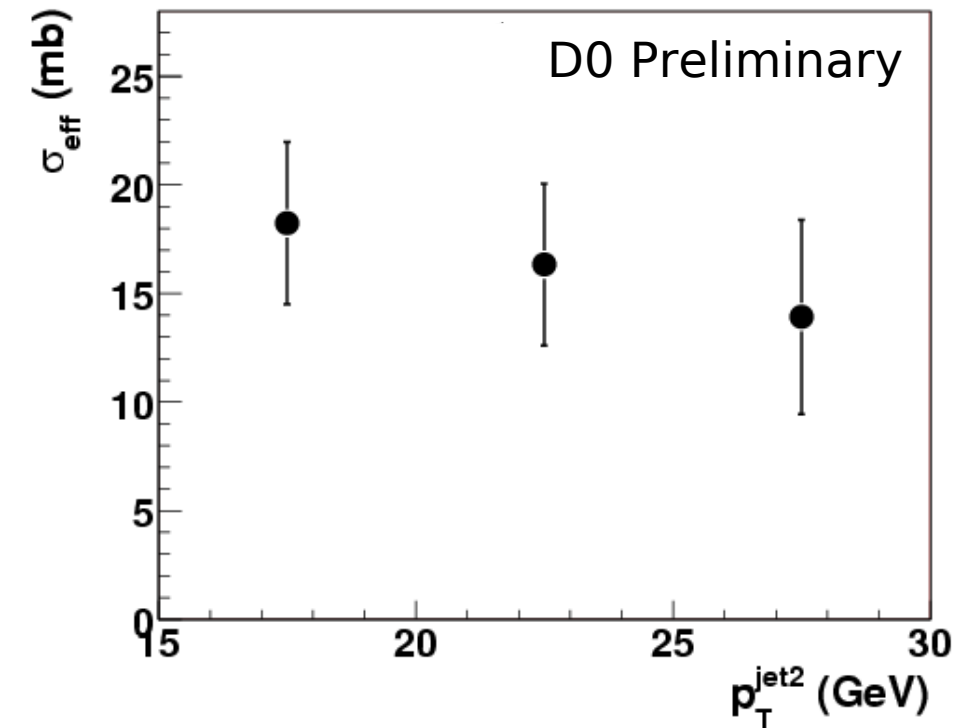
σ_{hard} is hard (non-elastic, non-diffractive) $p\bar{p}$ cross section.

It is 44.7 ± 2.9 mb : from Run I \rightarrow Run II extrapolation.

$$R_c = \frac{N_c(1)}{2N_c(2)} \sigma_{\text{hard}} = 52.3 \text{ mb}$$

Variation of σ_{hard} within uncertainty (2.9 mb) gives the uncertainty for R_c of just about 1.0 mb: increase of σ_{hard} leads to decrease of $N_c(1)/N_c(2)$ and vice versa.

Calculation of σ_{eff}



- σ_{eff} values in different jet p_T bins agree with each other within their uncertainties (also compatible with a slow decrease with p_T).
- Uncertainties have very small correlations between jet2 p_T bins.
- One can calculate the averaged (weighted by uncertainties) values over jet2 p_T bins:

$$\sigma_{\text{eff}}^{\text{ave}} = 16.4 \pm 0.3(\text{stat}) \pm 2.3(\text{syst}) \text{ mb}$$

Main systematic and statistical uncertainties (in %) for σ_{eff} .

p_T^{jet2} (GeV)	Systematic uncertainty sources					δ_{syst} (%)	δ_{stat} (%)	δ_{total} (%)
	f_{DP}	f_{DI}	$\varepsilon_{\text{DP}}/\varepsilon_{\text{DI}}$	JES	$R_c\sigma_{\text{hard}}$			
15 – 20	7.9	17.1	5.6	5.5	2.0	20.5	3.1	20.7
20 – 25	6.0	20.9	6.2	2.0	2.0	22.8	2.5	22.9
25 – 30	10.9	29.4	6.5	3.0	2.0	32.2	2.7	32.3

We have measured:

- **Fraction of Double Parton events** in three pT bins of 2nd jet : 15-20, 20-25, 25-30 GeV. It varies from about **0.47 at 15-20 GeV to 0.22 at 25-30 GeV**.
- **Effective cross section** (process-independent, defines rate of Double Parton events) σ_{eff} has been measured in the same jet pT bins with average value:

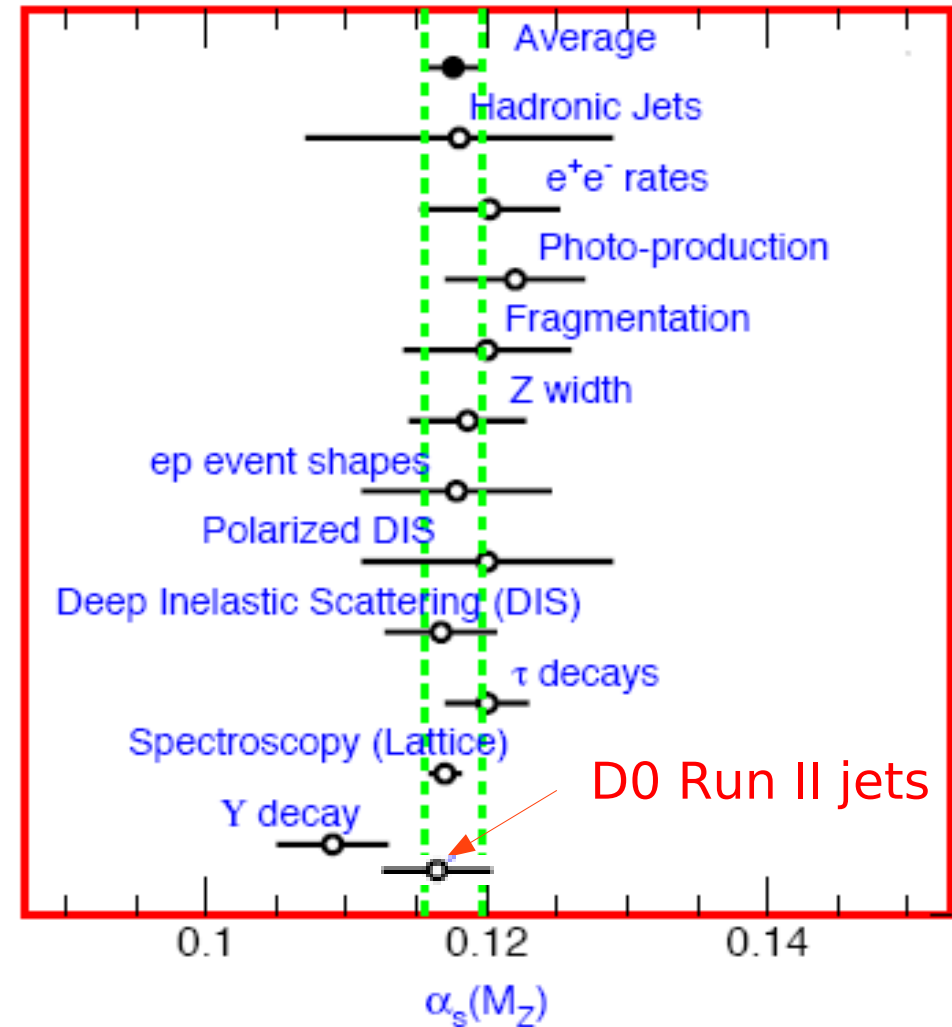
$$\sigma_{\text{eff}}^{\text{ave}} = 16.4 \pm 0.3(\text{stat}) \pm 2.3(\text{syst}) \text{ mb}$$

- The found σ_{eff} is in the range of those found in CDF measurements at lower scales
→ it might indicate a stable behaviour w.r.t. the energy scales in the parton scatterings.
- Double Parton production can be a significant background to many rare processes, especially with multi-jet final state. A choice of the dedicated variables is advised. It also necessitates tuning of MC generators, for which these results should be very helpful.

New α_s result from Tevatron
inclusive jet pT cross sections

$$\alpha_s(M_Z) = 0.1161^{+0.0041}_{-0.0048}$$

- Considerable improvement in comparison with accuracy of Run I jet result
- Similar precision as HERA jets (0.1189 ± 0.0032)
- Good agreement with the world average: 0.1184 ± 0.0007



BACK-UP SLIDES

Comparison of $\gamma+3$ jets measurements: CDF'97 vs. D0'09

- ✓ Center of mass energy : 1.8 \rightarrow 1.96 TeV
- ✓ About a factor 60 increase in the integrated luminosity allows to change selections:
 - photon $p_T > 16$ GeV (CDF) \rightarrow $60 < p_T < 80$ GeV (D0)
 - \Rightarrow A better separation of 2 partonic scatterings in the momentum space
 - \Rightarrow A higher photon purity (due to also tighter photon ID)
 - \Rightarrow A better determination of energy scales of 1st parton process
- ✓ Higher jet p_T s and JES correction to the particle level
 - Jet p_T (uncorr.) > 6 GeV \rightarrow p_T (corr.) > 15 GeV
- ✓ Binning in the 2nd jet p_T : 15 - 20; 20 - 25, 25 - 30 GeV
 - \Rightarrow A better determination of energy scales of 2nd process
 - \Rightarrow Study of Double Parton fractions and σ_{eff} vs. 2nd jet p_T
- ✓ Double Parton fractions and σ_{eff} are inclusive: we do not subtract fractions of events with triple parton interactions.

PDF correlations and σ_{eff}

- Correlations between PDFs are possible and may even *increase* DP cross section at large ($\geq W/Z$ mass) factorization scales (10-40%!):
 - A.M. Snigirev et al : PRD68 (2003)114012, PLB 594(2004)171
 - D. Treleani et al : PRD72 (2005)034032
- Direct account of PDFs is in DP PDF (!): *first* evolution equations for dPDF (extension of sPDF) --> J.Gaunt and J.Stirling, 0910.4347 [hep-ph]

dDGLAP evolution:

if the two-parton distributions are factorized at some scale μ_0

$$G(x_1, x_2, \mu_0) = G(x_1, \mu_0) * G(x_2, \mu_0)$$

then the evolution violates this factorization *inevitably* at any diff. scale $\mu \neq \mu_0$:

$$G(x_1, x_2, \mu) = G(x_1, \mu) * G(x_2, \mu) + R(x_1, x_2, \mu)$$

where $R(x_1, x_2, \mu)$ is a correlation term.

$$d\sigma = \sum_{q/g} \int \frac{d\sigma_{12} d\sigma_{34}}{2\sigma_{\text{eff}}} D_p(x_1, x_3) D_{\bar{p}}(x_2, x_4) dx_1 dx_2 dx_3 dx_4$$



$$\frac{\sigma_{DPS}^{\gamma+3j}}{\sigma^{\gamma j} \sigma^{j j}} = [\sigma_{\text{eff}}^{\text{exp}}]^{-1} \quad \Rightarrow \quad [\sigma_{\text{eff}}^{\text{exp}}]^{-1} = [\sigma_{\text{eff}}]^{-1} (1 + \delta(\mu))$$

Models of parton spatial density and σ_{eff}

- σ_{eff} is directly related with parameters of models of parton spatial density
- Three models have been considered: Solid sphere, Gaussian and Exponential.

TABLE VI: Parameters of parton spatial density models calculated from measured σ_{eff} .

Model for density	$\rho(r)$	σ_{eff}	R_{rms}	Parameter (fm)	R_{rms} (fm)
Solid Sphere	Constant, $r < r_p$	$4\pi r_p^2/2.2$	$\sqrt{3/5}r_p$	0.53 ± 0.06	0.41 ± 0.05
Gaussian	$e^{-r^2/2a^2}$	$8\pi a^2$	$\sqrt{3}a$	0.26 ± 0.03	0.44 ± 0.05
Exponential	$e^{-r/b}$	$28\pi b^2$	$\sqrt{12}b$	0.14 ± 0.02	0.47 ± 0.06

- The rms-radia above are calculated w/o account of possible parton spatial correlations. For example, for the Gaussian model one can write [Trleani, Galucci, 0901.3089,hep-ph]:

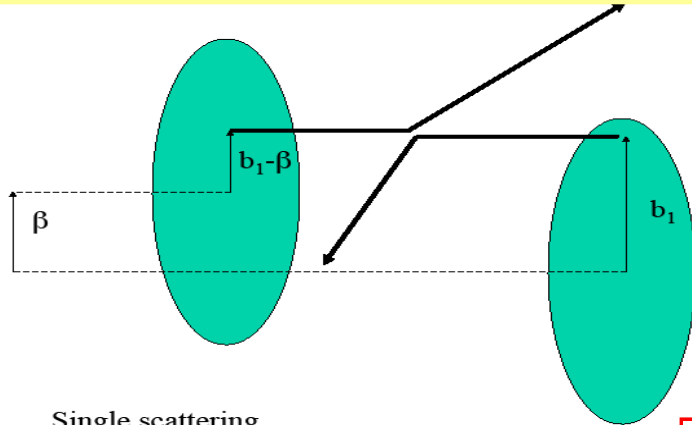
$$\frac{1}{\sigma_{\text{eff}}} = \frac{3}{8\pi R_{\text{rms}}^2} (1 + \text{Corr.})$$

- If we have rms-radia from some other source, one can estimate the size of the spatial correlations

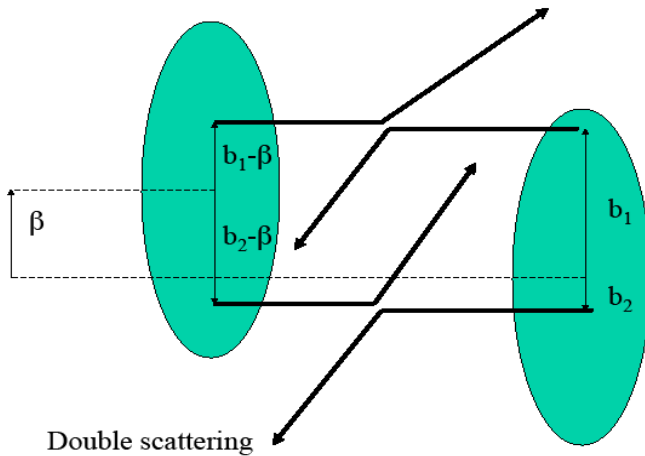
Parton spatial density and σ_{eff}

Introducing the 3D parton density $\Gamma(x, b)$ and making the assumption $\Gamma(x, b) = G(x)f(b)$ one may express the single scattering inclusive cross section as

$$\begin{aligned}\sigma_S &= \int_{p_t^c} G(x) \hat{\sigma}(x, x') G(x') dx dx' \\ &= \int_{p_t^c} G(x) f(b) \hat{\sigma}(x, x') G(x') f(b - \beta) d^2 b dx dx' d^2 \beta\end{aligned}$$



$$\begin{aligned}\sigma_D &= \frac{1}{2!} \int_{p_t^c} G(x_1) f(b_1) \hat{\sigma}(x_1, x'_1) G(x'_1) f(b_1 - \beta) d^2 b_1 dx_1 dx'_1 \times \\ &\quad \times G(x_2) f(b_2) \hat{\sigma}(x_2, x'_2) G(x'_2) f(b_2 - \beta) d^2 b_2 dx_2 dx'_2 d^2 \beta \\ &= \frac{1}{2!} \int \left(\int_{p_t^c} G(x) f(b) \hat{\sigma}(x, x') G(x') f(b - \beta) d^2 b dx dx' \right)^2 d^2 \beta \\ &= \frac{1}{2} \frac{\sigma_S^2}{\sigma_{\text{eff}}}\end{aligned}$$



where $\sigma_{\text{eff}}^{-1} = \int d^2 \beta [F(\beta)]^2$ is effective cross section

$$F(\beta) = \int f(b) f(b - \beta) d^2 b,$$

and $f(b)$ is the density of partons in transverse space.

1st and 2nd interactions: Estimates of possible correlations

... in the momentum space:

1st interaction: photon $p_T \simeq 70$ GeV, \Rightarrow parton $xT \simeq 0.07$

2nd interaction: jet $p_T \simeq 20$ GeV, \Rightarrow parton $xT \simeq 0.02$

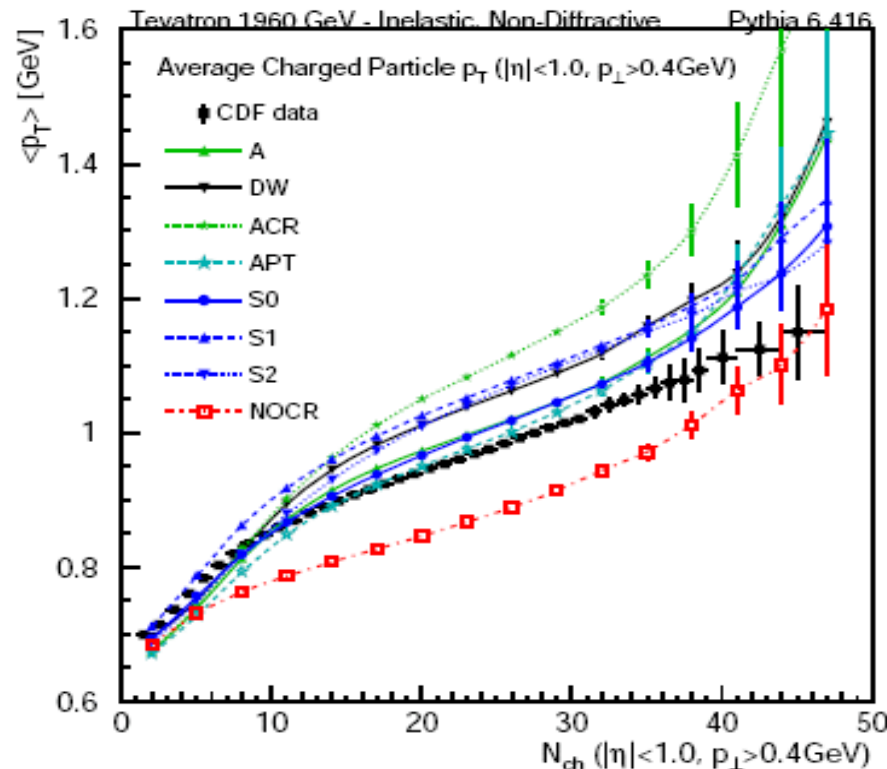
\Rightarrow large (almost unlimited) kinematic space for the 2nd interaction

... at the fragmentation stage :

\Rightarrow Simulate $\gamma+3$ jets and di-jets with switched off ISR/FSR; then additional 2 jets in $\gamma+3$ jets should be from 2nd parton interaction

\Rightarrow compare 2nd (3rd) jets p_T/Eta in $\gamma+3$ jets with 1st (2nd) jet p_T/Eta in dijets

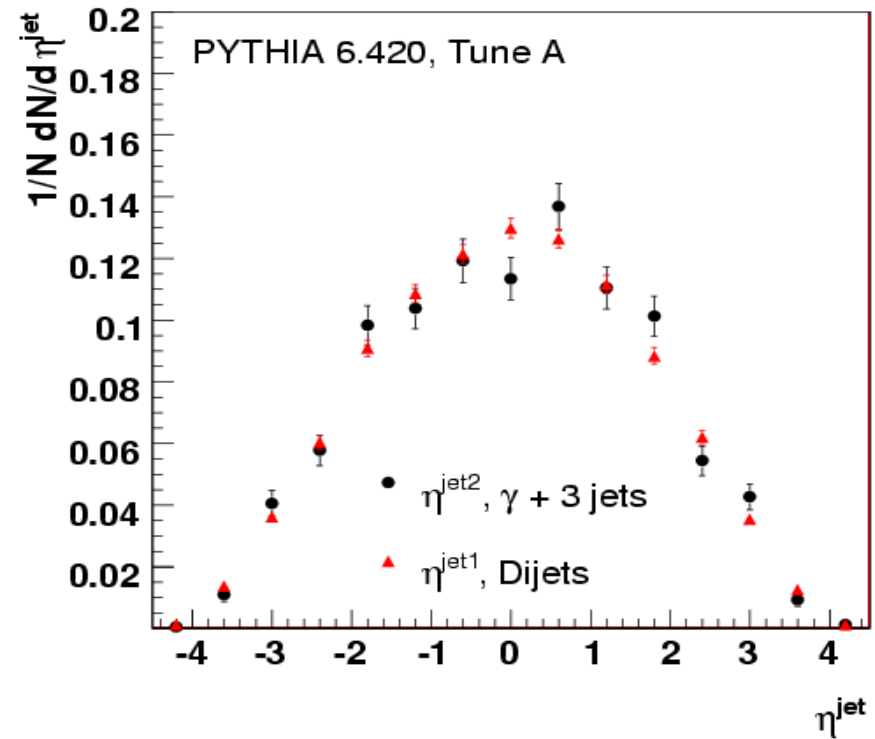
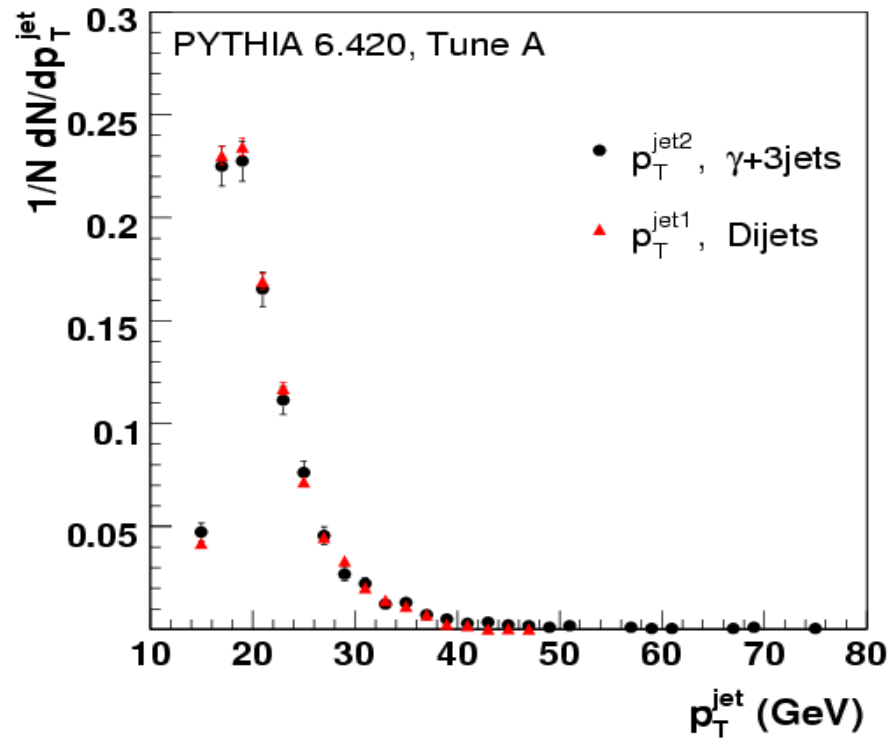
\Rightarrow Tunes tested: A, A-CR, S0



From D.Wicke &
P.Skands
hep-ph:0807.3248

γ +3 jets and di-jets, IFSR=OFF: jets pT comparison.

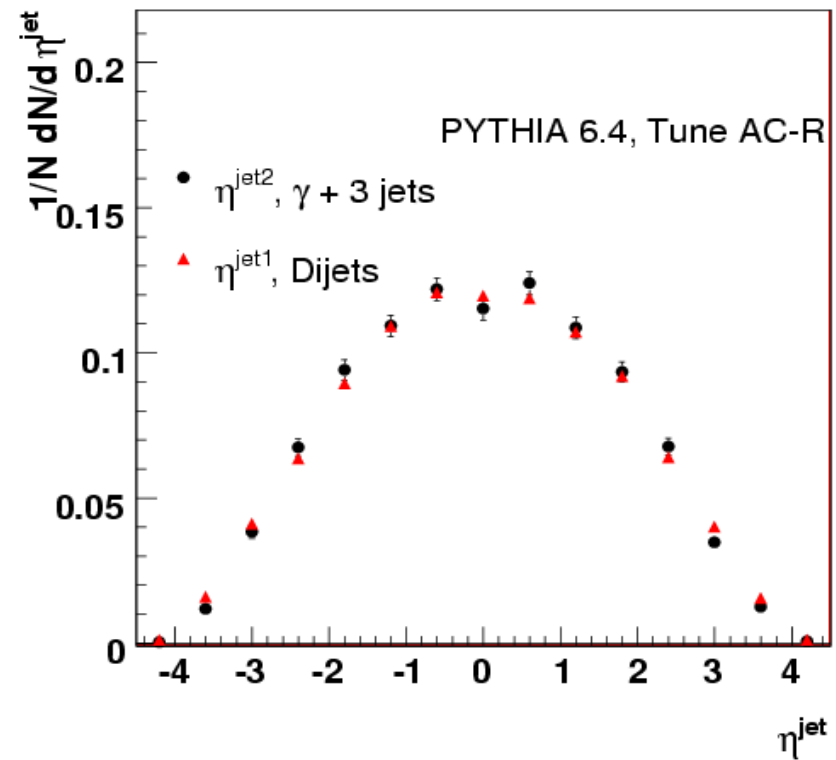
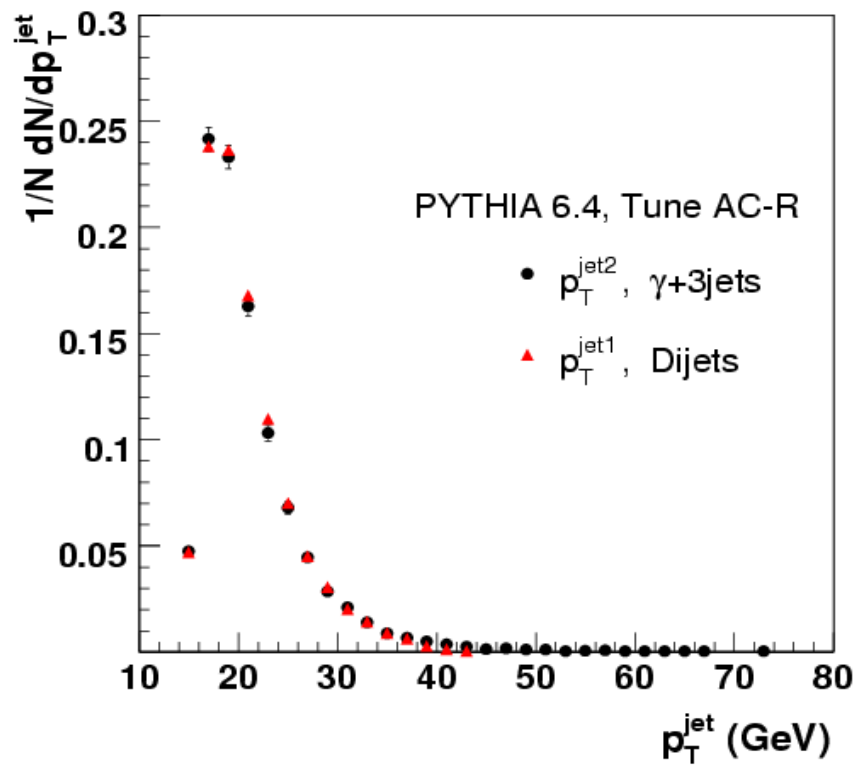
Tune A



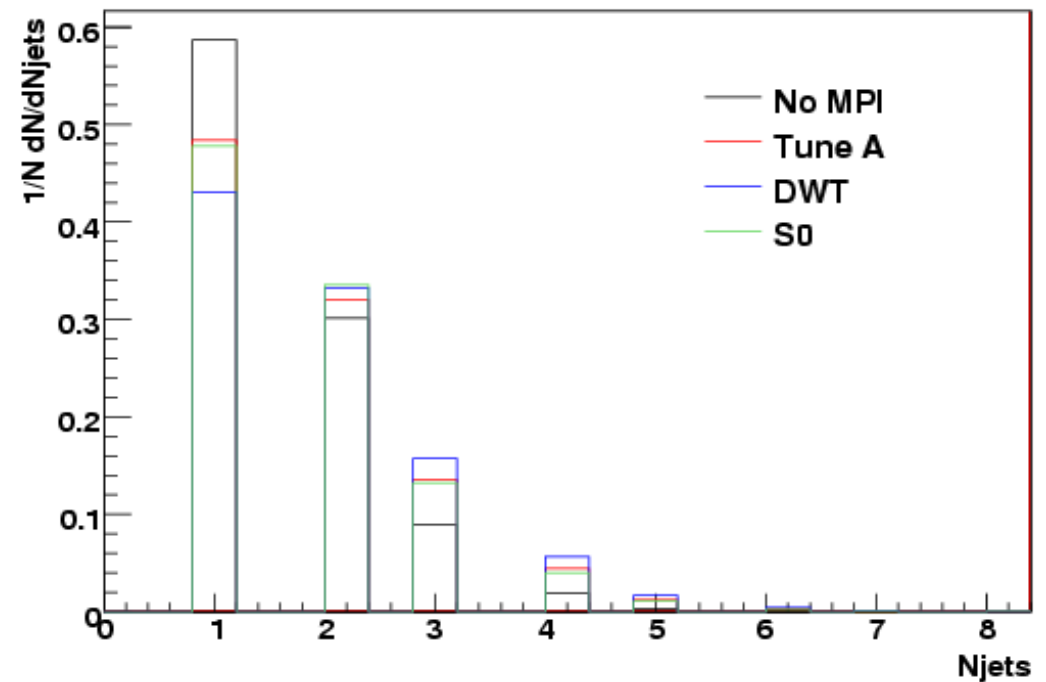
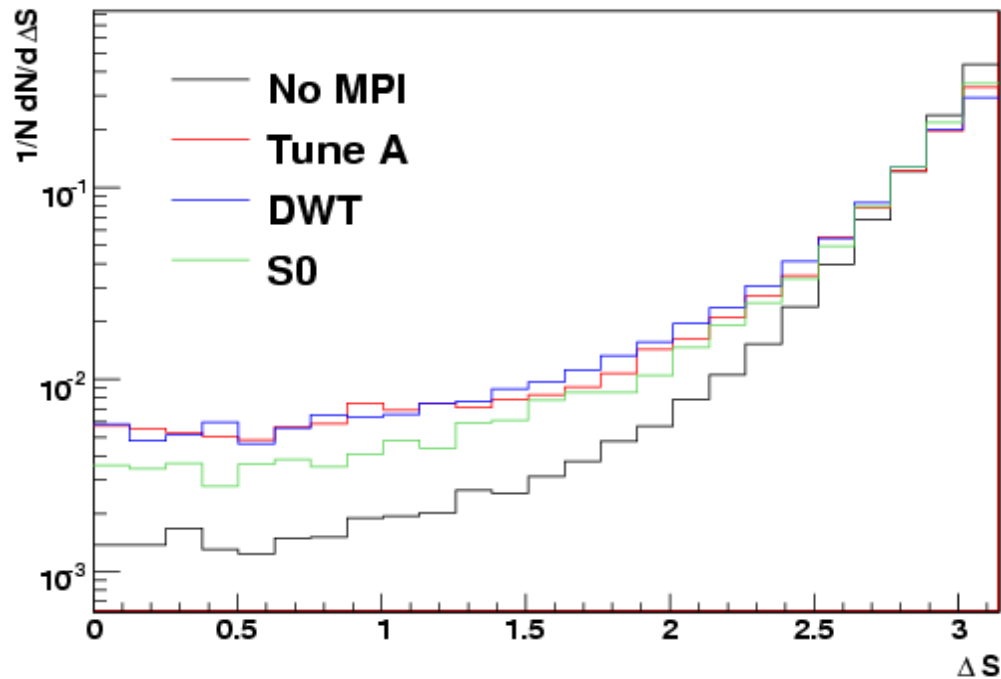
- pT and Eta distributions are analogous for jets from 2nd interaction in γ +3jets and di-jet events
- Analogous results (incl. 3rd jet from γ +3jets and 2nd from di-jets) are obtained for Tunes A-CR, S0.

γ +3 jets and di-jets, IFSR=OFF: jets pT comparison.

Tune A-CR



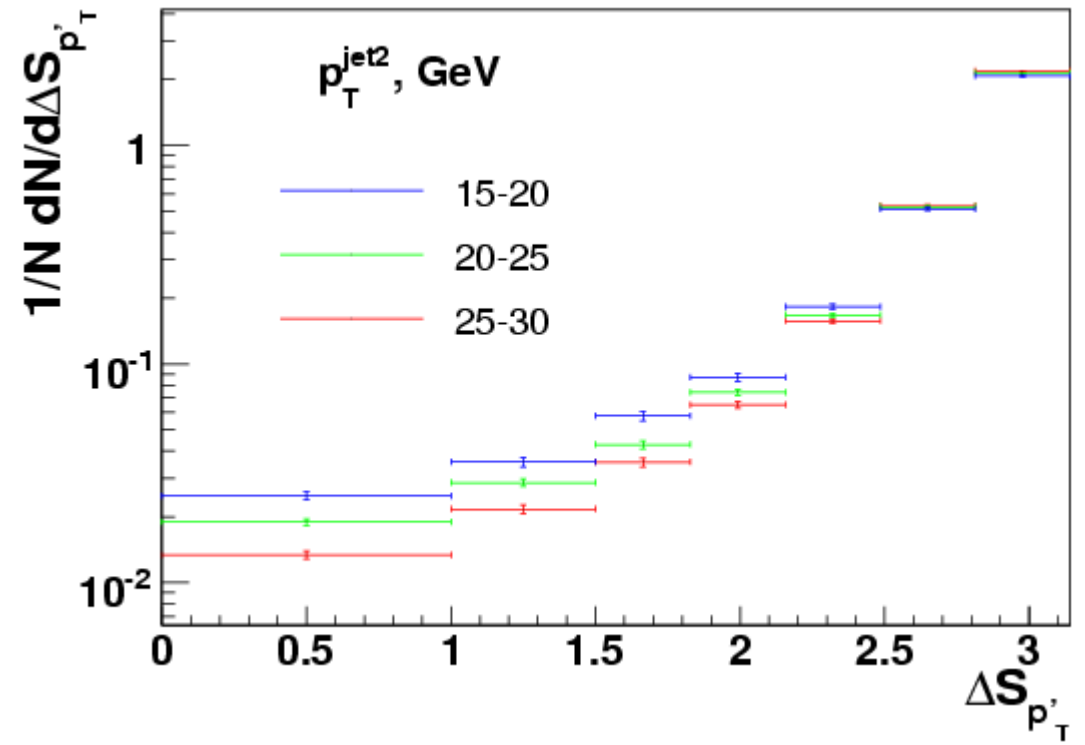
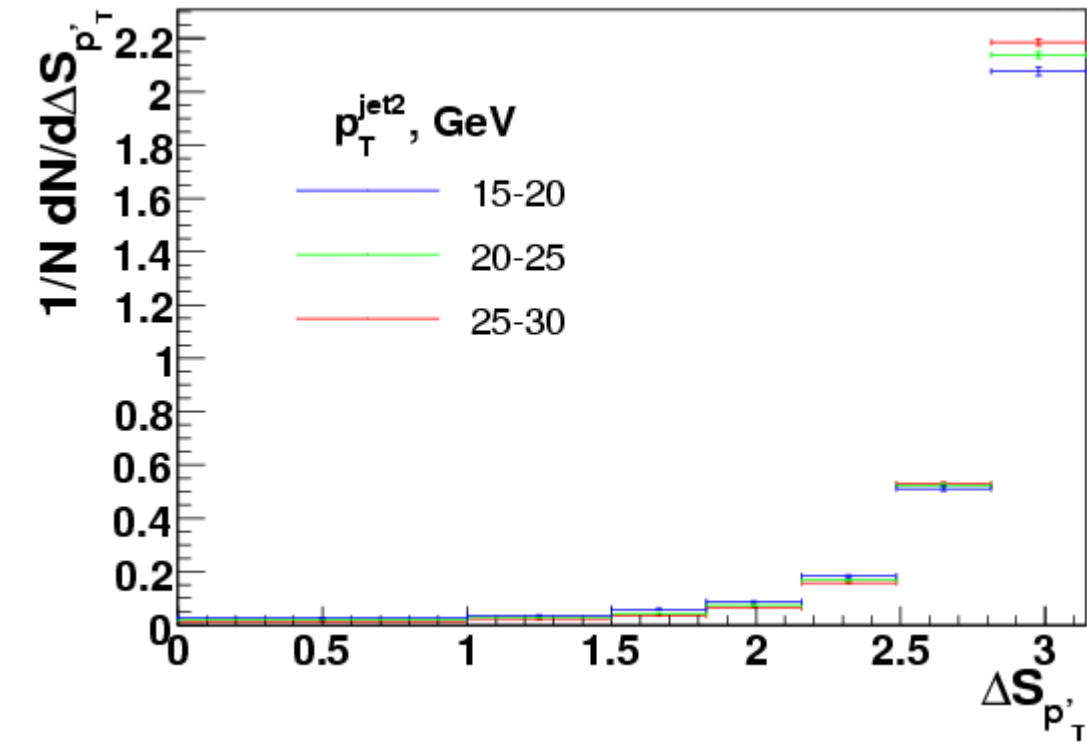
Pythia MPI Tunes: ΔS and Njets



Pythia predictions with MPI tunes:

- ΔS is much broader for events with MPI events and almost flat at $\Delta S < 1.5$
- $\#events(N_{jets} \geq 1) / \#events(N_{jets} \geq 3)$ is larger by a factor 2(!) for MPI events

SP events (Pythia): ΔS distributions



SELECTION CRITERIA

VERTEX:

- $|Z| < 60 \text{ cm}$,
- $N_{\text{trk}} \geq 3$

JETS (pT corrected):

- Midpoint Cone algo with $R=0.7$
- $|\eta| < 3.0$
- $\# \text{jets} \geq 3$
- pT of any jet $> 15 \text{ GeV}$
- pT of leading jet $> 25 \text{ GeV}$
- pT of 2nd jet $\in (15, 20), (20, 25), (25, 30) \text{ GeV}$.

PHOTONS:

- photons with $|\eta| < 1.0$ and $1.5 < |\eta| < 2.5$
- $60 < pT < 80 \text{ GeV}$ (good separation of 1st and 2nd parton interactions)
- Shower shape cuts
- Calo isolation ($0.2 < dR < 0.4$) < 0.07
- Track isolation ($0.05 < dR < 0.4$) $< 1.5 \text{ GeV}$
- Track matching probability < 0.001

- $\Delta R(\text{any objects pair}) > 0.7$